Optimization of Design and Analysis of Y-Axis Spindle for SB CNC-30 Machine

Prof. Issac Thamban¹, Bessy Paul², Vysakh R Nair³, Peter Siby⁴, Cijo Saju⁵, Sanal P P⁶

¹Professor, Department of Mechanical Engineering, Mar Athanasius College of Engineering, Kerala, India.
²Deputy Engineer, Design Section, Hindustan Machine Tools Ltd, Kalamassery, Kerala, India.
³⁴⁵⁶Department of Mechanical Engineering, Mar Athanasius College of Engineering, Kerala, India.

Abstract – Spindles are used to provide a relative motion between the work piece and the tool. Usually when the spindles are designed its dimensions may not be optimized. This may result in greater vibration and induction of stress which results in poor machining accuracy.

The project aims to optimise the existing y-axis spindle design of SB CNC 30 machine so as to achieve improved accuracy of rotation for a prescribed rigidity of spindle unit. This also includes determination of critical speed and strength of the spindle. This project deals with optimisation of outer spindle diameter and span length between the bearings ensuring maximum static and dynamic stiffness and minimum deflection.

Key Words: Spindle, SB CNC 30 machine, static stiffness, optimization, modal analysis, Von-Mises stress.

1. INTRODUCTION

A machine tool is composed of basic components: spindle, moving axes and a cutting tool. Among these components, spindle is almost the most critical one due to its vital duty in the metal cutting process. The basic purpose of spindle is rotating either the workpiece or the cutter with enough torque and speed against the other which is fixed to enable the cutting happen. An internal driven motor is used to provide the required drive to the spindle. Such spindles have built-in electric motors inside the housing coupled with the spindle shaft.

Because spindle shaft is the main rotating component of the system and one of the first component to withstand the loads during cutting, its stiffness and robustness greatly affect both static and dynamic behaviour of the spindle system and ultimately the performance of the machine. The basic spindle structure consists of housing, bearings, motor and a spindle shaft. The spindle structure and its components arrangement are shown in the figure 1.1. The bearings used in the design are angular contact ball bearings and cylindrical roller bearings due to its high radial load capacity, rigidity and low coefficient of friction.

In this research we are optimising the span length between the bearings and outer diameter of the spindle for a prescribed rigidity of the spindle unit and accuracy of spindle rotation. Optimization is done for the y-axis spindle of SB CNC 30 machine. SB refers to slant bed and CNC 30 refers to the model name. The research also extends to the determination of critical speed of the spindle.

The spindle is considered as a beam which is supported between the bearings with a net load acting at the overhanging section. This net load comprises of weight of chuck, weight of job, tangential and radial cutting forces.

Optimization is carried out so as to satisfy two conditions.

1. Minimum deflection at the overhanging section.

Some of the assumptions followed while designing the spindle are as follows.

(a) The test shaft is assumed to be Euler-Bernoulli beam.
(b) Both the beam and bearings act according to Hooke's law.
(c) Any torsional and axial deflections of the shaft are neglected.
(d) Deflections and slopes are small.
(e) The bearing housings are assumed to have infinite stiffness.
(f) The contribution of transverse shear deformation to the overall lateral deflection is assumed to be negligible.
(g) Deflections do not change the behavior of the loads or reactions.

Fig.1.1: Basic lathe spindle structure.
1.2 Material Used.

The material used for spindle is C2R toughened steel (15Ni7Cr4Mo2) and its chemical composition is given below:

1. Carbon C(%) = 0.15  
2. Silicon Si(%) = 0.23  
3. Manganese Mn(%) = 0.5  
4. Phosphorous P(%) = 0.040  
5. Sulphur S(%) = 0.040  
6. Copper C(%) = 0.025  
7. Chromium Cr(%) = 0.10  
8. Nickled Ni(%) = 0.011  
9. Tin Sn(%) = 0.05

The material attains its required toughness and hardness after a number of heat treatment processes like carburising, annealing, normalising, hardening and toughening. This is achieved by passing and dipping the spindle in carburising bath, hardening bath, annealing bath and quenching bath in the heat treatment section. Approximate contents in carburising bath are sodium cyanide (8-10%), sodium chloride and barium chloride at working temperature of 910°C. Hardening bath (850°C) and annealing bath (650°C) comprises of sodium chloride and barium chloride while quenching bath consist of sodium nitrite and sodium nitrate at a temperature of 180°C. Mechanical properties of C2R toughened steel are shown in Table 1.2.1.

The spindle is then analyzed both statically and dynamically. The static analysis mainly focuses on the spindle deflection and stiffness in the loaded case, which is the worst-case machining scenario. The distances between the bearings, or the support locations on the spindle shaft, directly affect the spindle static stiffness, therefore in the static analyses, investigation and selection of optimum bearing spans within an applicable range is calculated analytically. These optimum values are used in the further analyses and the final design. And finally in the dynamic analysis, the modes, natural frequencies and the critical speeds of the design are investigated.

Static analysis was carried out using Finite Element Method (FEM) with the software ANSYS Workbench 16.0. Stress, strain and deflection of the spindle are determined using this method. Dynamic analysis was done using ANSYS Mechanical APDL 16.2.

2. METHODOLOGY

The objective of this research is to optimize the span length between the bearings and outer diameter of the spindle for a prescribed rigidity of the spindle unit and accuracy of spindle rotation. The research also extends to the determination of critical speed of the spindle.

First design calculations for the spindle and bearings were carried out for optimizing the span length and outer diameter of spindle using CMT design handbook and bearing catalogues. Microsoft Excel sheet was used to carry out several iterations and to arrive at optimum results. Optimization was carried out so as to satisfy two conditions.

1. Minimum deflection at the overhanging section.  

Inner diameter of the spindle is kept constant throughout (d=103 mm) and outer diameter is varied. The spindle is considered as a beam which is supported between the bearings with a net load acting at the overhanging section. This net load comprises of weight of job, weight of chuck, tangential and cutting forces.

The spindle is then modeled using Creo Parametric 2.0. as shown in figure 2.1.

Fig 2.1: Spindle modeled using Creo Parametric 2.0.
Fig. 2.1.1: Load diagram of spindle bearing system.

$R_a$ and $R_b$ are the reactions exerted by cylindrical roller bearing and angular contact ball bearings respectively.

Resolving forces in vertical direction,

$$R_A + F = R_B$$

$$R_B - R_A = 1036.4216 \quad \text{(i)}$$

At equilibrium, $\sum M = 0$

$$R_A (318.99 + 154.55) - 154.55R_B = 0$$

$$\therefore R_B = 3.06399 \quad R_A \quad \text{(ii)}$$

Solving (i) and (ii)

$$R_A = 502.14468 \text{ kgf}$$

$$R_B = 1538.566 \text{ kgf}$$

Inner spindle diameter and overhanging length are kept constant throughout as 103 mm and 154.55 mm respectively. Initially the span length between bearings is taken as 318.99 mm which needs to be optimized. The span length between the bearings and outer spindle diameter is to be optimized. A triple row angular contact ball bearing (front bearings) is mounted near the spindle nose and a double row cylindrical roller bearing (rear bearing) is mounted at the other end.

Spindle rigidity $j$ is given by,

$$j = \frac{F}{Y} = \frac{1}{K + \frac{1}{j_1} + \frac{1}{j_2} + \frac{1}{j_B}} \quad \text{kgf/mm}$$

where $k = l/a$ is the ratio of span length (l) to overhanging length (a), $j_A$ and $j_B$ are the rigidity of the cylindrical roller bearing and angular contact ball bearing respectively and Y is the deflection at the overhanging section. Once spindle rigidity is determined, deflection can be determined using $j=F/Y$.

Bearings are designed using CMT design handbook and SKF bearing catalogues. Numerically optimum span length and optimum outer diameter of spindle are obtained by changing the distance between bearings and outer diameter of spindle simultaneously, so that deflection of the spindle at overhanging section is minimum and static stiffness is maximum. The number of rows of bearings are also changed to arrive at optimum results. These iterations are done using Microsoft Excel.

The first critical speed of the shaft is given by,

$$N_{cr} = \frac{1}{\sqrt{W I^2}} \quad \text{rpm}$$

Where I is the moment of inertia of spindle, $l$ is the span length and $w=66.80486 \text{ kgf}$ is the weight of the shaft, C is a constant and is equal to $13.5 \times 10^6 \text{ for simply supported beams}$.

### 2.2 Static analysis and optimization

During machining, spindle experiences various loads due to cutting, centrifugal effects, etc. These loads may invoke self-excited vibrations and may cause spindle failure due to high deformation and high stresses generated. Therefore, the spindle design should be analyzed and verified statically and dynamically. The static analysis of the spindle basically deals with the spindle stiffness which is closely related to the load capacity and vibration resistance of the spindle. It also helps to analyze the accuracy loss during limit pushing cutting operations.

In this research, the preliminary spindle design is analyzed both statically and dynamically. The static analysis mainly focuses on the spindle deflection and stiffness in the loaded case, which represents the maximum load conditions. Static analysis is done in ANSYS Workbench 16.0 which includes determination of optimum span length and optimum outer diameter. Here the position of angular contact ball bearing is fixed and position of cylindrical roller bearing is changed along the spindle length. Deflection is analyzed at each position and span length corresponding to minimum deflection was chosen as the optimum span length. The results from static analysis are then compared with those obtained from numerical calculations.

### 2.3 Dynamic analysis

Every spindle experiences vibration due to the nature of cutting operation, but the severity of the vibration greatly influences the machining accuracy, the life of cutting tool and spindle, cutting power necessary for the operation. Thus, dynamic analysis is important to investigate and understand the spindle modal behavior.

Due to the nature of the machining operation, a periodic cutting force is generated on the spindle which produces a continuous cyclic response. The elastic properties of the tool, material or the spindle causes this harmonic behavior in the cutting force. If the frequency of the exciting cutting force is the same as the spindle inherent frequency then resonance will occur during its operation. Resonance leads to chatter and vibrations with extreme amplitudes. It greatly affects the precision of the process and even leads to spindle and bearing failures due to high cyclic loads generated in the structure. Therefore in the cutting operations, the resonance
should always be avoided no matter what the source is, spindle, cutting tool, fixture, etc. In modal analysis, the modes, natural frequencies and the critical speeds of the design are investigated.

3. RESULTS AND DISCUSSIONS.

In this work results from both numerical calculations and that obtained from FEA (Finite Element Analysis) method are compared so as to arrive at optimum results. Maximum static stiffness and minimum deflection at the overhanging section are satisfied during optimization. Thus stress induced in the spindle are minimum and within the yield limit. Hence spindle and bearing failure does not occur during machining.

3.1 Using design calculations.

The results obtained using numerical calculations are shown in the following table.

<table>
<thead>
<tr>
<th>SL NO</th>
<th>Parameters</th>
<th>Before Optimization</th>
<th>After Optimization</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Outer spindle diameter</td>
<td>160 mm</td>
<td>180 mm</td>
</tr>
<tr>
<td>2</td>
<td>Span length between bearings</td>
<td>318.99 mm</td>
<td>463.65 mm</td>
</tr>
<tr>
<td>3</td>
<td>Stiffness of spindle</td>
<td>0.4114*10⁹ N/m</td>
<td>0.785*10⁹ N/m</td>
</tr>
<tr>
<td>4</td>
<td>Deflection at the overhanging section</td>
<td>24.71 µm</td>
<td>12.9 µm</td>
</tr>
</tbody>
</table>

Table.3.1.1: Results of analytical method.

Thus by changing the outer spindle diameter from 160 to 180 mm and the span length from 318.99 mm to 463.65 mm stiffness of spindle increases and deflection at the overhanging section reduces. Thus optimum outer diameter is 180 mm and optimum span length is 463.65 mm.

3.2 Using FEA method

During machining, both in axial and lateral directions, cutting forces are generated on the spindle. However, in most cases, lateral loads are greater than the axial loads, and similarly the axial stiffness of the spindle is greater than the bending stiffness. Therefore, especially for lathe spindles, it is more important to investigate the lateral loading of the spindle in the static analysis. In this research, only lateral deflection and bending stiffness are studied and calculated.

Structural analysis was carried out using FEA method with the software ANSYS Workbench 16.0. Stress, strain and deflection of the spindle are determined using this method. This method involves dividing the entire structure into smaller elements of finite dimensions which are connected together at finite number of joints called nodes. This process is called mesh formation. The results of analysis before optimization are shown in the following figures.

Fig.3.2.1: Variation of shear stress before optimization.

Fig.3.2.2: Variation of total deformation before optimization.

Fig.3.2.3: Variation of Von-Mises stress before optimization.

Figures 3.2.4, 3.2.5 and 3.2.6 shows the results of analysis after optimization.
The results from structural analysis show that maximum deformation occurs at the overhanging section where the net load is acting. The results obtained using FEA method are shown in table 3.2.1.

<table>
<thead>
<tr>
<th>SL NO</th>
<th>Parameters</th>
<th>Before optimization</th>
<th>After optimization</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Outer spindle diameter</td>
<td>160 mm</td>
<td>170 mm</td>
</tr>
<tr>
<td>2</td>
<td>Span length between bearings</td>
<td>318.99 mm</td>
<td>386.47 mm</td>
</tr>
<tr>
<td>3</td>
<td>Stiffness of spindle</td>
<td>3.829*10^9 N/m</td>
<td>4.8186*10^9 N/m</td>
</tr>
<tr>
<td>4</td>
<td>Deflection at the overhanging section</td>
<td>2.655 µm</td>
<td>2.11 µm</td>
</tr>
<tr>
<td>5</td>
<td>Maximum equivalent stress</td>
<td>6.652 MPa</td>
<td>4.3411 MPa</td>
</tr>
</tbody>
</table>

Table 3.2.1: Results of FEA method.

Thus using FEA method, optimum outer diameter is 170 mm and optimum span length is 386.47 mm. The spindle shaft only experiences elastic deformation under the cutting forces studied. As shown in figure 3.2.5, the maximum von-Mises stresses generated in the shaft are at the bearing locations and have the value of 4.34 MPa, which is fairly below 588.6 MPa, the yield strength of C2R steel-spindle shaft material. Therefore, the shaft is sufficient to carry the loads without any plastic deformation or failure and no plastic deformation is expected during cutting operations.

There are variations in the values obtained using FEA method and analytical method. However, for both the cases, bearing span length directly affects the static stiffness of spindle. The deviation in the values may be due to the assumptions followed for the analytical method. The analytical model is still found useful for the optimization of bearing spans and understanding the behavior of spindle rigidity. However, for better estimations of the deflection and rigidity, FEM solution and results should be used.

Optimization of spindle design also results in improved accuracy of rotation with high dynamic stiffness and minimum deflection. Thus machining accuracy can be improved.

### 3.3 Modal analysis

The dynamic analysis of the preliminary spindle design is done using ANSYS Mechanical APDL 16.2. The analysis is performed with the same simplified spindle model used in the static FEM analyses. The eigen frequencies of the spindle calculated for the first 10 modes and the corresponding speeds in rpm are given in table 3.3.1.

<table>
<thead>
<tr>
<th>Modes</th>
<th>Frequency (Hz)</th>
<th>Speed (Rpm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1st</td>
<td>12.5893</td>
<td>755.358</td>
</tr>
<tr>
<td>2nd</td>
<td>12.6187</td>
<td>757.122</td>
</tr>
<tr>
<td>3rd</td>
<td>19.9369</td>
<td>1196.214</td>
</tr>
<tr>
<td>4th</td>
<td>19.9780</td>
<td>1198.68</td>
</tr>
</tbody>
</table>
Table 3.3.1: Natural frequencies and speeds for different modes.

In addition to the determination of natural frequencies and critical speeds, modal analysis also determines the mode shapes for each frequency. The mode shapes for the first 6 modes are shown in the following figures.
The 1st and 2nd eigen frequencies of the spindle are same and mutually orthogonal, and can be considered as multiple roots, as shown in figures 3.3.1 and 3.3.2. 1st natural frequency is the bending mode of the spindle in Y direction, while 2nd is the bending mode in X direction. 3rd natural frequency represents the deflection of spindle section in X direction and 4th mode represents axial deformation at section away from the spindle nose. 5th mode represents rotation about Z-axis at the overhanging section and 6th mode represents deflection in Y direction between the bearing supports.

The working speed range for the spindle is 28-2800 rpm and first mode occurs at 755.358 rpm and 10th mode occurs at 1645.164 rpm. Thus natural frequency of spindle coincides with external excitation frequency and resonance is found to occur at these modes and in between these modes corresponding to the critical frequencies. Resonance results in vibration of the spindle at very high amplitudes and decreases the precision of the process and even results in spindle and bearing failures due to high cyclic loads generated in the structure. Hence to avoid resonance the spindle should be operated below 755 rpm.

4. CONCLUSIONS

Spindle deflection under the cutting forces primarily affects the accuracy and the life rating of the spindle. Moreover, lower deflection and higher precision are usually demanded in finishing cuts, which have lower chip thicknesses and higher speeds, and lower cutting forces as result. Since the maximum Von-Mises stress generated in the spindle are much below the yield strength of C2R spindle-shaft material, no plastic deformation and failure of spindle and bearings occur during operation. This improves accuracy of rotation with high dynamic stiffness and minimum deflection. Thus machining accuracy also improves. The deviation in the values obtained using FEA method and analytical method may be due to the assumptions followed for the analytical method. However, for the cases, bearing span length directly affects the static stiffness of spindle.

Modal analysis shows that the spindle should be operated below 755 rpm so as to avoid the danger of vibration due to resonance. Hence the spindle is suitable for medium speed applications.

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