

Fuel cell based distributed generation using Re-lift Luo converter

Vijayalakshmi A¹

Independent scholar, Power Electronics and Industrial Drives, No.25,Dr.Varadarajan street, Vedachalam Nagar, Chengalpet, Tamilnadu, India,

Abstract – In this paper fuel cell based distributed generation for driving the brushless dc motor is presented. The low voltage extracted from the fuel cell has been increased to the utility voltage using re-lift Super-lift technique. The proposed converter with a simple structure effectively enhances voltage transfer gain, promising high efficiency and power density solution using single active switch, producing reduced ripple voltage and current. The working operation of the proposed converter has been discussed in detail. The Solid oxide fuel cell (SOFC) mathematical modeling has been presented for constant fuel utilization. Both the open-loop and closed loop control strategies are presented under different load-torque condition for the drive system. The conventional PI controller is devised for closed loop control operation and its performances are evaluated using Simulink/ Matlab platform.

Key Words: Distributed generation, Relift super-lift technique, SOFC, Constant fuel utilization.

1. INTRODUCTION

The progress of any nation primarily depends on the energy sector which paves way for socio-economic up-liftment of the people. But the ever-demanding energy consumption threatens the depleting conventional fossil fuels, increasing global warming and greenhouse gas emissions. So energy harnessing should be met by other alternate renewable energy sources to curtail the energy crisis problem and global warming issues. Fuel cell technology is one among the renewable promising a safe, clean, eco-friendly, reliable and sustainable energy solution. They are electrochemical devices that convert chemical energy into electrical energy directly in a single stage processing. Thus they are simpler, flexible, and modular when compared to conventional power plants. They operate silently without any moving parts and combustion of gas resulting zero emission of greenhouse gases. The other advantages include their placement sites independent of geographic boundaries, not intermittent in nature, featuring high efficiency, even at part-load conditions. Thus they are suitable for power generation promoting the energy security and can be connected to the power grid to provide supplemental power. They also function as a standalone on-site power generator for ranches, dairy farms, flower growers and residences which are located far off from the power utilities [1].

1.1 Problem Statement

A dc-dc converter accepts a low voltage, high current input from the fuel cells and convert the power to a high

voltage output [3]. But this green technology powered by the fuel cell is limited by its sluggish response to the sudden load changes [10] with high ac ripples in its output dc voltage. So the major challenge lies in the development and selection of a suitable ripple mitigating power conditioning unit (PCU) to compensate for these limitations and its applicability to interface to the power utility applications. The PCU is thus the prime topic of this paper.

1.2 Power Conditioning Unit

The success of the power conditioning unit vests in the performance of the dc-dc converter to meet the demand requirements, ability to cope with the fuel cell behavior ensuring safe and stable operation despite the voltage variations. The transformer based DC-DC converters such as fly-back converter, push-pull converter, forward converter, half-bridge converter, bridge converter, and Zeta converter suffer from reduced overall operating efficiency due to leakage inductance, core loss. The inclusion of a transformer increases the operational cost, installation space and weight. They add objectionable ripples in the current flowing out of the fuel cell [8], besides the power switch of these converters is subjected to high voltage stress due to the leakage inductance of the transformer. Hence transformer-less DC-DC converters are of prime choice.

2. PROPOSED CONVERTER TOPOLOGY

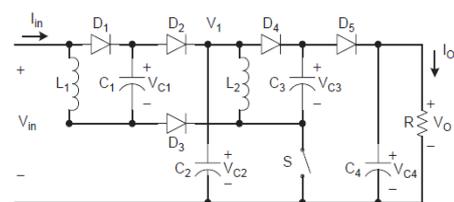


Fig -1: P/O SL Luo converter Re-lift circuit

The re-lift Luo converter analysed in this paper is a series of advanced step-up dc-dc power conversion topologies based on the super-lift (SL) technique, which increases the output voltage stage-by-stage in geometric series using a simple structure[2]. This technique effectively enhances the voltage transfer gains besides mitigating the effects of parasitic elements for wide range of duty ratio[1]. They provide high efficient and high power density solution with reduced ripple voltage and current. The conventional cascade boost DC-DC converters utilizes 'n' no of power switches for n stages of power conversion while in the re-lift Luo converter only one power switch is incorporated

reducing the circuit control complexity, gate drive requirements, switching losses thus enhancing the converter efficiency, involving less no of protective circuits, cooling, making the converter simple, compact in size. The positive output super-lift Luo re-lift converter shown in Fig.1 consists of only one static switch S, five diodes, four capacitors and two inductors.

2.1 Circuit Operation

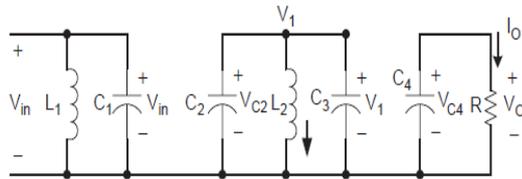


Fig -2: Equivalent circuit of the converter during switch-on mode of operation

When the power switch S is turned on, the diodes D₁, D₃, D₄ are on and the equivalent circuit during switch-on condition is obtained. During switch-on period, the first elementary power stage composed of L₁-D₁-D₃-C₁ is charged by the input source voltage V_{in}. The voltage V₁ which is the output voltage of the elementary power stage appears across capacitor C₂. It is given by

$$V_{C2} = V_1 = \left[\frac{(2-k)}{(1-k)} \right] V_{in} \quad (1)$$

The voltage re-lift power conversion is obtained by the topology formed by the inductor L₂ and the capacitor C₃ to form a parallel connected pump circuit (super-lift pump) to absorb the stored energy from the preceding stage of the capacitor C₂. Thus the capacitor C₃ is charged to V₁ during the switch on mode period.

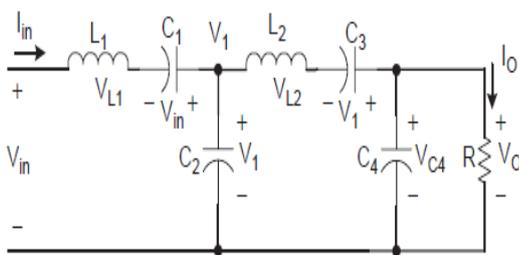


Fig -3: Equivalent circuit of the converter during switch-off mode of operation

When the power switch S is turned off, the diodes D₂, D₅ are on and the equivalent circuit during switch-off condition is obtained. During switch-off mode of operation, L₁ is in series with capacitor C₁ in the first power stage. The energy stored in the elementary Luo pump is transferred to the capacitor C₂. The voltage V₁ which is the output voltage of the elementary power stage appears across capacitor C₂. Similarly L₂ is in series with capacitor C₃. The energy stored in the second stage Luo pump of the re-lift circuit is

transferred to the capacitor C₄. Now the re-lift boost voltage V_{re-lift} appears across capacitor C₄. It is given by

$$V_{C4} = V_{re-lift} = \left(\left[\frac{(2-k)}{(1-k)} \right] V_{in} \right)^2 \quad (2)$$

Thus the capacitors C₁ and C₃ function as storage capacitors. The capacitors C₂ and C₄ act as support capacitors. During switch-on mode of operation, the current in inductor L₂ increases with voltage V₁ for a period of kT while it decreases with voltage (V_o-2V₁) for a period of (1-k)T during switch-off mode of operation.

$$\frac{V_1 k T}{L_2} = \frac{(V_o - 2V_1)(1-k)T}{L_2} \quad (3)$$

The output voltage V_o is given by

$$V_o = \left(\frac{(2-k)}{(1-k)} \right) V_1 \quad (4)$$

The output voltage V_o in terms of input voltage is given by

$$V_o = \left(\frac{(2-k)}{(1-k)} \right)^2 V_{in} \quad (5)$$

The Voltage transfer gain is M = $\frac{V_o}{V_{in}}$

$$= \left[\frac{(2-k)}{(1-k)} \right]^2 \quad (6)$$

Hence, the expressions for ripples in inductor current and current through inductor are obtained as under.

The peak to peak current ripple in the inductor is the same during steady state operation and it is given as:

$$\Delta i_{L2} = \frac{V_1 k T}{L_2} = \frac{(V_o - 2V_1)(1-k)T}{L_2} \quad (7)$$

$$L_2 = \left[\frac{(2-k)}{(1-k)} - 1 \right] I_o = \frac{I_o}{(1-k)} \quad (8)$$

$$\Delta i_{L1} = \frac{V_{in} k T}{L_1} \quad (9)$$

$$I_{L1} = \frac{I_{in}}{(2-k)} \quad (10)$$

Therefore the variation ratio of inductor current L₁ is

$$\xi_1 = \frac{\Delta i_{L1}/2}{I_{L1}} = \frac{k(2-k)TV_{in}}{2L_1 I_{in}} = \frac{k(1-k)^4 4R}{2(2-k)^3 f L_1} \quad (11)$$

Similarly the variation ratio of inductor current L₂ is

$$\begin{aligned} \xi_2 &= \frac{\Delta i_{L2}/2}{I_{L2}} = \frac{k(1-k)TV_1}{2L_2 I_o} = \frac{k(1-k)^2 TV_o}{2(2-k)L_2 I_o} \\ &= \frac{k(1-k)^2 R}{2(2-k)fL_2} \end{aligned} \quad (12)$$

The variation ratio of the output voltage is

$$\epsilon = \frac{\Delta v_o/2}{V_o} = \frac{1-k}{2RfC_4} \quad (13)$$

3. SYSTEM DESCRIPTION

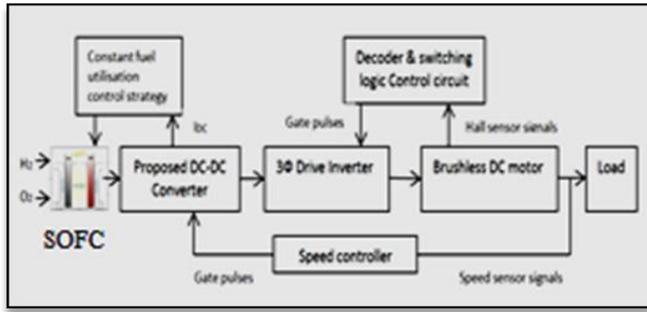


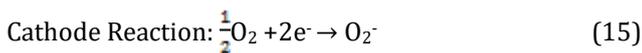
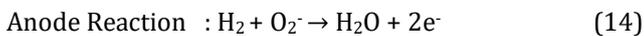
Fig -4: Block diagram of the proposed system

Figure 4 shows the general block diagram of the proposed system. The proposed fuel cell geared drive system consists of a Solid Oxide fuel cell stack, re-lift Luo converter, inverter with a control circuit for driving the Brushless-dc motor coupled load.

3.1 Solid Oxide Fuel Cell

SOFCs are highly instant reactive efficient fuel cell variants which reduces corrosion and heat management problems. It paves way for a more economical system using Ni in place of costly Platinum, thus tolerating carbon monoxide emission and its flexibility to feed any other forms of fuel, either hydrogen or hydrocarbon derived fuels.

Each of the electrode reactions constitutes a half-reaction [4].



The overall chemical reaction that takes place inside the fuel stack is given as



The assumptions made for the fuel cell model are given as:

- The fuel cell reactions are assumed to be in equilibrium.
- The cathode and anode inlet and exit temperature of the fuel cell is assumed to be equal.
- The gases behave as ideal gases.
- Gas leakage is negligible.

3.2 Solid Oxide Fuel Cell Mathematical Modeling

The developed SOFC model is based on the reference [9]. Gibbs' free energy is referred to as the energy extracted from the fuel cell to do external work, regardless of any change in pressure or volume of the fuel reactants and products. Under standard operating conditions of temperature of 25°C and pressure of 0.1 MPa the change in Gibbs' free energy of formation per mole is given as

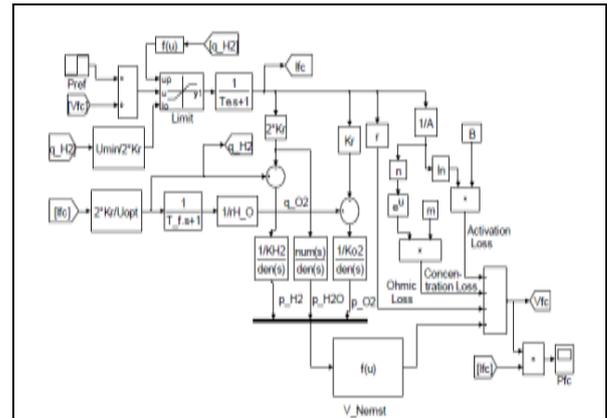


Fig -5: SOFC mathematical modelling

$$\Delta \bar{g}^f = (\bar{g}^f)_{H_2O} - (\bar{g}^f)_{H_2} - \frac{1}{2} (\bar{g}^f)_{O_2} \quad (17)$$

The reversible open circuit voltage in terms of the Gibb's free energy of formation is given as

$$E^o = -\frac{\Delta \bar{g}^f}{2F} \quad \text{where } F = 96.487 \times 10^6 \text{ J/kmol} \quad (18)$$

The change in Gibbs' free energy $\Delta \bar{g}^f$ varies from its STP value with changes in pressure and temperature which eventually leads to change in stack voltage of the fuel cell.

$$\Delta \bar{g}^f = \Delta \bar{g}^f{}^o - RT \ln\left(\frac{p_{H_2} p_{O_2}^{0.5}}{p_{H_2O}}\right) \quad (19)$$

Where R- Universal gas constant=8314 J/ (kmol K)

T - Operating temperature

p_{H_2} - partial pressure of hydrogen

p_{O_2} - partial pressure of oxygen

p_{H_2O} - partial pressure of water

Using (19) in (20) yields Nernst voltage at standard temperature with varying pressure values.

$$E = E^o + \frac{RT}{2F} \ln\left(\frac{p_{H_2} p_{O_2}^{0.5}}{p_{H_2O}}\right) \quad (20)$$

Fuel flow utilization factor is given from [5] as,

$$U_f = \frac{\text{Amount of fuel (H}_2\text{) that reacts with O}_2}{\text{Amount of fuel (H}_2\text{) which enters the anode}} \\ = \frac{q_{H_2 \text{ react}}}{q_{H_2 \text{ inside}}} = \frac{mf_{H_2 \text{ react}}}{mf_{H_2 \text{ inside}}} \quad (21)$$

Where $q_{H_2}^{\text{react}}$ - molar flow rate of hydrogen reacting with the oxygen.

$q_{H_2}^{\text{inside}}$ - molar flow rate of hydrogen entering the anode.

To calculate partial pressure of gases, Ideal gas law is used.

For hydrogen, $p_{H_2} V_{an} = n H_2 RT$

$$pH_2 = \frac{n H_2 RT}{V_{an}} \tag{22}$$

$$qH_2^{inside} = \frac{2K_r I_{fc}}{0.85} \tag{34}$$

V_{an} - Volume of anode channel

nH_2 - hydrogen moles in the channel

Taking the first-order derivative of the above equation yields,

$$\frac{d}{dt} (pH_2) = \frac{d}{dt} \left(\frac{n H_2 RT}{V_{an}} \right) = \frac{qH_2 RT}{V_{an}} \tag{23}$$

$$\frac{d}{dt} (pH_2) = \frac{RT}{V_{an}} [qH_2^{inside} - qH_2^{outside} - qH_2^{react}] \tag{24}$$

The amount of hydrogen reacts depends upon the demand load current and the total capacity of the no of cells connected in series with the stack which is given as,

$$qH_2^{react} = \frac{N_o I_{fc}}{2F} \tag{25}$$

Being N_o and $2F$ are numericals,

$$qH_2^{react} \propto I_{fc} = 2K_r I_{fc} \tag{26}$$

Where N_o - no of cells connected in series

I_{fc} - fuel cell current

$$K_r - \text{modelling const} = \frac{N_o}{4F}$$

Upon substituting and integrating on both sides of the equation and upon Laplace transformation yields

$$pH_2 = \frac{3/k_{H_2}}{1 + \tau H_2} [qH_2^{inside} - 2K_r I_{fc}] \tag{27}$$

$$\text{Similarly } pO_2 = \frac{3/k_{O_2}}{1 + \tau O_2} [qO_2^{inside} - 2K_r I_{fc}] \tag{28}$$

$$pH_2O = \frac{3/k_{H_2O}}{1 + \tau H_2O} [qH_2O^{inside} - 2K_r I_{fc}] \tag{29}$$

$$\text{where } \tau H_2 = \frac{V_{an}}{kH_2 RT} \tag{30}$$

Nernst stack voltage is given from [6],

$$V_{fc} = E_{fc} - V_{activation} - V_{ohmic} - V_{conc} \tag{31}$$

$$\text{Where } E_{fc} = N_o \left\{ E^0 + \frac{RT}{2F} \ln \left(\frac{pH_2 pO_2^{0.5}}{pH_2O} \right) \right\} \tag{32}$$

3.2 Constant Fuel Utilization mode of Operation

The fuel cell operation is carried out in constant fuel utilization mode. To prevent overused and underused fuel conditions, U_f is set between 0.8 and 0.9 for better performance [9]. So demand current I_{fc} is limited within the range

$$\frac{0.8qH_2^{inside}}{2K_r} \leq I_{fc} \leq \frac{0.9qH_2^{inside}}{2K_r} \tag{33}$$

The fuel utilization is maintained at about 85% for optimal performance by tracking the output stack current and adjusting the input fuel flow rate.

3.3 Brushless DC Drive system

The high performance featured work horse Brushless dc motor is chosen for our simulation study. Table.1 shows the switching logic used for electronic commutation.

Table -1: Switching logic in Brushless DC drive system

switching pattern	Hall signals			Decoder signal			Gate drive signals					
	h_a	h_b	h_c	emf_a	emf_b	emf_c	Q_1	Q_2	Q_3	Q_4	Q_5	Q_6
#1	0	0	1	0	-1	+1	0	0	0	1	1	0
#2	0	1	0	-1	+1	0	0	1	1	0	0	0
#3	0	1	1	-1	0	+1	0	1	0	0	1	0
#4	1	0	0	+1	0	-1	1	0	0	0	0	1
#5	1	0	1	+1	-1	0	1	0	0	1	0	0
#6	1	1	0	0	+1	-1	0	0	1	0	0	1

4. SIMULATION RESULTS

The simulation has been developed for the SOFC fed brushless drive system using re-lift Super lift technique with parameters listed in Table1, Table 2 and Table 3.

Table -1: Proposed Converter parameters

Name of the parameters	Parametric Notation	Value
Input voltage	V_{in}	57 V
Output voltage	V_{out}	513 V
Inductor	L_1, L_2	100µH
Capacitor	C_1, C_2, C_3	5µf
Capacitor	C_4	100 µf
Switching frequency	f	50 KHz
Conduction Duty ratio range	k	0.3 to 0.9
Used Conduction Duty ratio	k	0.5

Table -2: SOFC model parameters

Parametric indices	Values
Universal gas constant	8314 J/(kmol K)
Faraday's constant	96.487x10 ⁶ J/kmol
Ideal standard potential	1.18 V
Ohmic loss polarization for each cell	3.2813x10 ⁻⁴ ohm
Absolute stack temperature	1273 K
Air inlet temperature (pre-heated)	773 K

Fuel compressor pressure	100 psi
Air blower pressure	3 atm pressure
Initial fuel cell stack current	100 A
No of cells arranged serially	65
Maximum fuel flow utilization	90%
Minimum fuel flow utilization	80%
Optimum fuel flow utilization	85%
Molar constant for hydrogen	8.43×10^{-4} kmol/S.atm
Molar constant for Oxygen	2.52×10^{-3} kmol/S.atm
Molar constant for water	2.81×10^{-4} kmol/S.atm
Ratio of hydrogen to oxygen	1.145
Response time of fuel processor	5 sec
Electrical Response time	0.8 sec

Table -3: Brushless dc motor model parameters

Parametric indices	Symbols	Values
Stator resistance per phase	R_s	2.8750 ohm
Stator inductance per phase	L_s	8.5 mH
No. of poles pairs	$p/2$	4
Moment of inertia	J	0.8×10^{-3} Kg m^2
Friction coefficient	F	1×10^{-3} Nms
Voltage constant	K_v	56.8335V/rpm
Torque constant	K_T	0.54372 Nm-A
Flux established by magnets	Φ	0.06784 V.s

4.1 Open loop control of BLDC motor

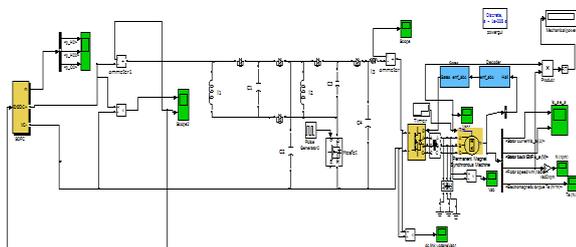


Fig -6: Open-loop control of the BLDC drive system

Case: 1 Steady-state operating condition.

The simulation is performed for constant load torque of about 3 Nm and the performances are evaluated. Figure 7 shows the rotor speed of the drive system for the applied constant load torque.



Fig -7: Rotor speed for constant load torque

Figure 8 shows the drive generated electro-magnetic torque.

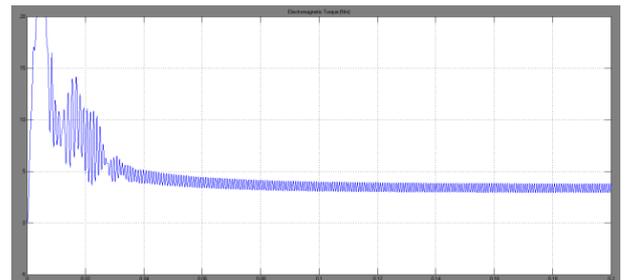


Fig -8: Motor torque for constant load torque

Figure 9 and figure 10 shows the corresponding stator per-phase current, back-emf waveforms and the inverter output voltage waveforms.

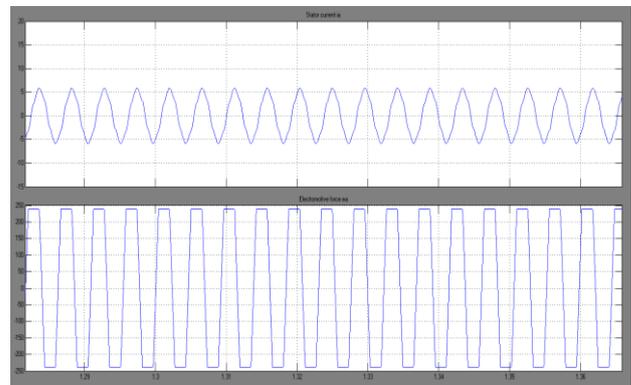


Fig -9: Stator per-phase current, motor back-emf for constant load torque

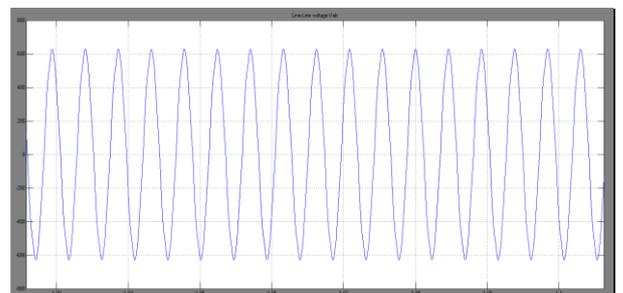


Fig -10: Inverter output voltage

Figure 11 and figure12 shows the drive dc link voltage and the proposed converter current.

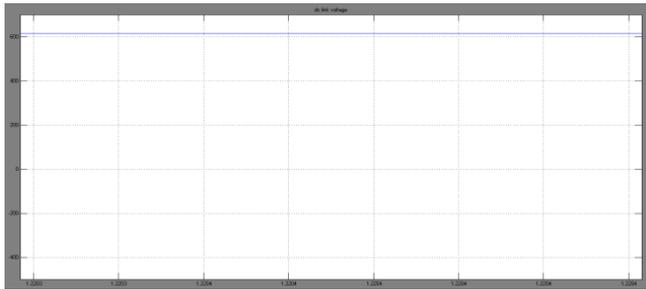


Fig -11: Drive dc link voltage

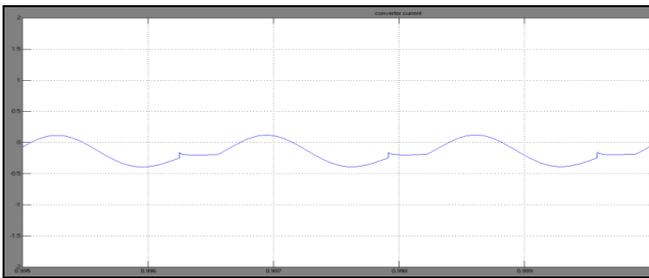


Fig -12: Proposed converter current

Case 2: Dynamic load torque disturbances

The simulation is performed for load torque variation of 0 Nm to 1 Nm and to 3 Nm at time t=0 sec, 1 sec and 2 sec respectively and the drive's response is studied under open loop system. The observed changes are the drop in inverter output voltage shown in figure 13, dynamic speed changes of the rotor seen in figure 14.

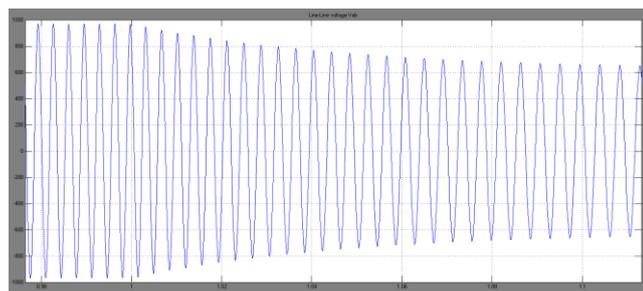


Fig -13: Drop in inverter output voltage from the time of load torque variation

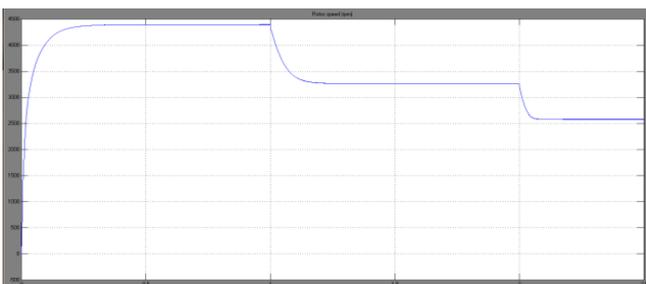


Fig -14: Speed variation due to load torque disturbances

Figure 15 shows the corresponding changes in stator currents and the back-emf waveforms and the figure 16 shows the dynamically developed motor torque under variable load torque conditions.

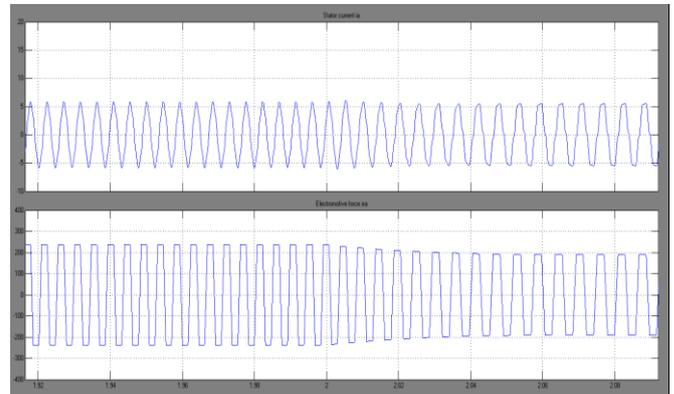


Fig -15: Stator per-phase current and the back-emf waveform variation

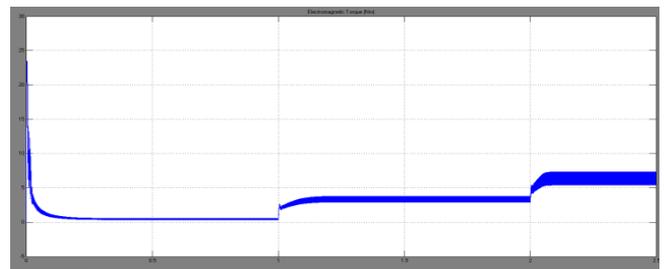


Fig -16: Developed motor torque under variable load torque condition

4.2 Closed loop Speed control of BLDC motor

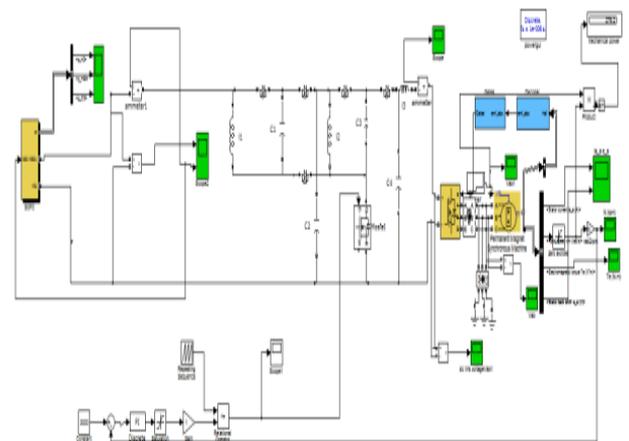


Fig -17: Closed loop simulation with PI control.

To tackle the load torque disturbances and source voltage variations, to have a constant speed control for the drive PI controller is implemented. The PI controller parameters chosen are $K_p = 0.001205$ and $K_i = 0.018$. The desired reference speed of the drive system is implemented by a Proportional-Integral speed controller. The error signal

which is the difference between the actual and desired speeds is given to the PI controller, which adjusts the duty cycle of the PWM generator which in turn adjust the corresponding re-lift Luo converter voltage required to maintain the desired speed.

The load torque variation is presented at about t=1 sec from 0 Nm to 3 Nm. and from 3 Nm to 5 Nm at t=2 sec. The PI controller is able to dynamically handle these changes and thus robust in its control action maintaining the speed to the set speed reference.

Figure 18 shows the constant drive speed accomplishment of PI controller control action under dynamically load torque variations. The desired speed is attained with the transients vanishing out quickly for every torque variations.

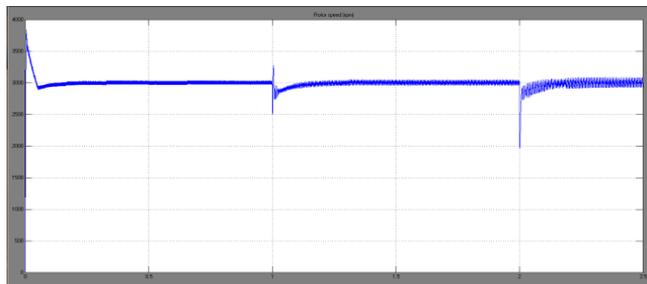


Fig -18: PI control producing constant drive speed

Figure 19 and figure 20 shows the motor's stator per-phase current, back-emf per-phase waveform and the developed drive torque.

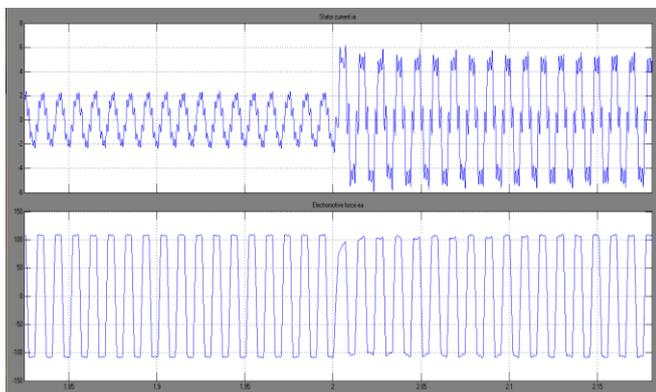


Fig -19: motor's stator per-phase current ,back-emf per-phase waveform

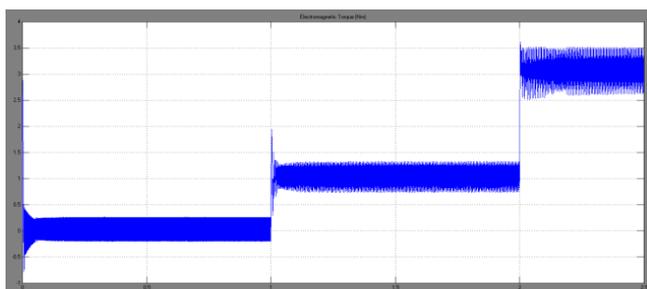


Fig -20: Developed drive torque

The FFT analysis shown in the figure 21 was performed for the drive output voltage and the THD observed was 3.83% which is well below 5% of the IEEE standard of harmonic limits.

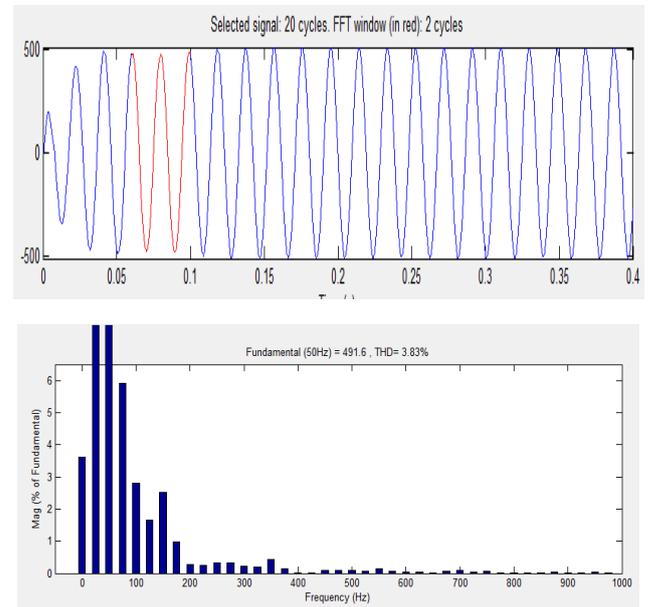


Fig -21: FFT analysis for the output voltage for the developed system

Table -1: Performances indices of the proposed P/O SL Luo converter Re-lift circuit

Parameter	Results Obtained
$V_{fuel\ cell}$	57 V
$I_{fuel\ cell}$	200 A
Output voltage V_0	513 V
Voltage transfer gain M	9
Peak to peak current ripple Δi_{L1}	1.71 A
Peak to peak ripple current Δi_{L2}	0.57 A
Steady state current in L2, IL_2	400 A
Steady state current in L1, IL_1	133.33 A
Variation ratio of inductor current L_1, ξ_1	2.137×10^{-3}
Variation ratio of inductor current L_2, ξ_2	2.137×10^{-3}
Variation ratio of the output voltage, ϵ	1.267×10^{-4}

5. CONCLUSION

In this paper, the proposed relift Luo converter with a simple construction utilizing only a single switch guaranting reduced switching loss is implemented to produce a high voltage transfer gain, stable and ripple free output. A constant fuel utilization mode is designed for increased fuel cell performance by the load current tracking scheme. The proposed power conditioning unit along with the PI

controller has the ability to cope with the slow fuel cell behavior, satisfies the dynamic load demand requirements ensuring safe, stable operation and accomplishes a desired speed control for the drive system. Thus the proposed re-lift Luo converter can be considered as an efficient interface for Solid oxide fuel cell distributed generation.

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