

# Development of *AlGaAs /GaAs/ AlGaAs* Step Quantum well to produce Tunable Photo Detector and Electro-Absorption Modulator for noise reduction

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**Abstract:** We design a Step Asymmetric Quantum well with *AlGaAs /GaAs/ AlGaAs* material. We derive the expression of absorption coefficient, which is important in the development of Tunable Photo Detector and Electro-Absorption Modulator. The “staircase” potential method was used to present both the effects of external bias and the shift in the detection wavelength due to the various applied external electric fields across the asymmetric quantum well. The electro absorption optical modulator is an optical modulator that utilizes the electroabsorption effect that the optical Absorption Coefficient of a substance varies depending on the electric field applied to it.

optical modulator is an optical modulator that utilizes the electro absorption effect that the optical Absorption Coefficient of substance varies depending on the electric field applied to it. [6]

## 1. Introduction:

## 2. Step asymmetric quantum well:

Epitaxial crystal growth techniques such as Molecular beam epitaxy or MOCVD allows to have monolayer upto 3 armstrong control in the chemical composition of the crystal. Nearly every semiconductor crystal such as GaAs, AlGaAs have been grown by epitaxial growth. This allows the growth of Quantum well where electronic properties can be altered. Quantum well systems are used for high performance devices such as transistors, lasers, modulators. Quantum wells offer a very useful approach to band structure tailoring. In quantum wells electrons behave as if they are in a 2-dimension space and acquire properties that are specially useful for many optoelectronic application.

Step quantum well can also be called a staircase structure. This type of structure consists of a stack of quantum wells. When the quantum well is adequately deep and narrow, its energy states are quantized. The potential depth and width of the well can be adjusted so that it has only two energy states: a ground state near the well bottom and a first excited state near the well top. If an external bias is applied in this type of quantum well, a reasonable amount of photocurrent is produced. [4] In Figure 2.1, photoexcited electron transition from the ground state to the first excited state, where an externally applied voltage sweeps them out, producing a photocurrent.

We are taking an AlGaAs-GaAs-AlGaAs material. Here a step asymmetric quantum well is formed by sandwiching an ultrathin film of AlGaAs in between two GaN layers.

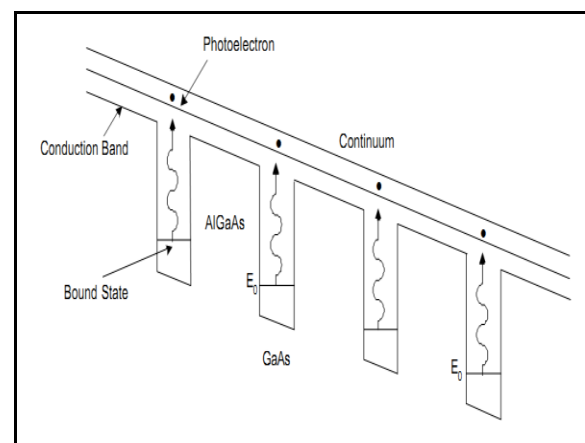


Fig 2.1: Electron excitation of asymmetric quantum well

For two bound states in the quantum well, only photons having energies corresponding to the energy separation between the

two states are absorbed, resulting in a photodetector with a sharp absorption spectrum. If there is only one bound state in the well, the transition occurs between the bound state and the continuum, producing a broader peak.[5]

Now designing a quantum well to detect light of a particular wavelength becomes a straightforward matter of adjusting the potential depth and width of the well to produce two states, separated by the desired photon energy.

The Schrödinger equation is solved numerically using the transfer matrix approach. In this case the Figure 2.2 is taken into account. The effect of the electric field on the energy levels will be incorporated by the "staircase" approximation of the linear potential

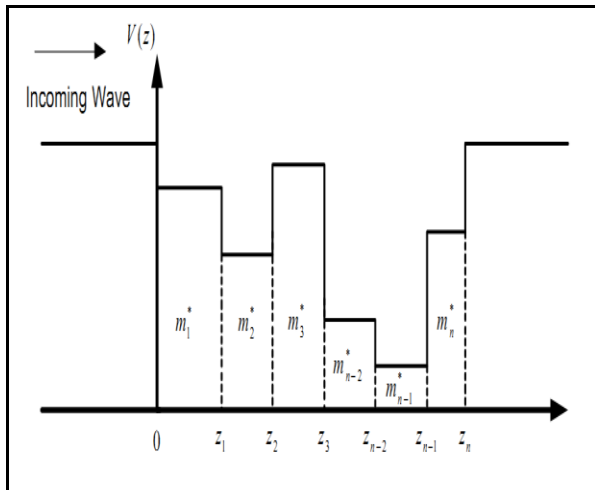


Fig 2.2: Arbitrary multi-layered potential well structure

### 2.1: Intersubband transition selection rules:

The first selection rule of intersubband transition is the parity selection rule. From Equation [2] it is found that the parity of the final state has to be different from that of the initial state in order to obtain a non-zero transition matrix element. This means that the intersubband transitions in a square quantum well can occur only from odd states to even states or vice versa. For example 1 to 2 or 2 to 3 transitions are allowed whereas 1 to 3 is not allowed. Figure 2.3 shows schematically the parity selection rule of the intersubband transitions in a square potential well. However, the symmetry of a square well can be broken by applying a relatively strong electric field, making the normally "forbidden" transitions become allowed

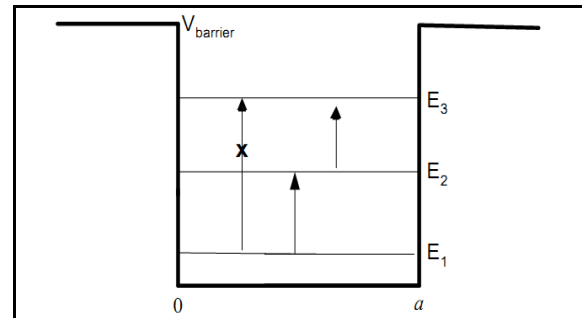


Figure 2.3: Square Quantum well showing allowed and forbidden transitions.

The second selection rule is the polarization selection rule. Since the potential modulation of a quantum well structure is only in one direction, the  $z$  direction, intersubband transition will not occur when the photon polarization is perpendicular to the  $z$  direction. This can be understood by considering the  $\cos q$  term in Equation This unique polarization selection rule is an important characteristic and can be used for the identification of the intersubband transition. In order to obtain a strong intersubband transition, the photon polarization has to coincide with the growth direction (i.e.,  $q = 0$ ).

For an asymmetric quantum well (see Figure 2.4), the dipole matrix elements of transitions for both odd-to-odd and even-to-even quantum numbers do not vanish, since the eigenfunctions of these energy states are not eigenfunctions of the parity operator.[1]

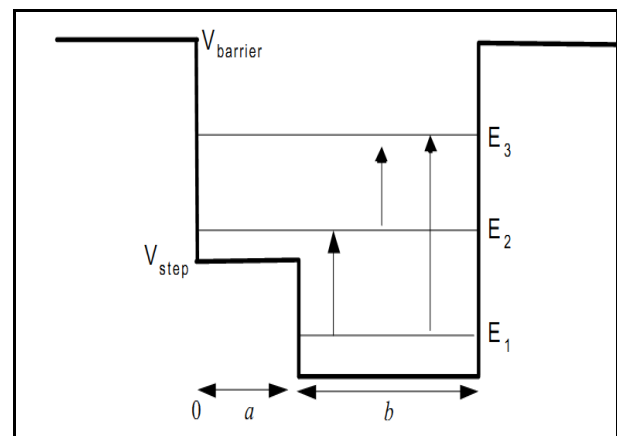


Fig 2.4 :Asymmetric quantum well with allowed transitions.

In addition to allowing intersubband transitions between any low states, the asymmetric well structure also gives linear Stark shift. This can be utilized for tuning the detection wavelength and also in electroabsorption optical modulator.

### 2.3. Intersubband absorption coefficient:

The absorption coefficient in quantum well devices is one of the most important factor in the design of the quantum structures and is proportional to the amount of incident light that is absorbed in the structure. The absorption coefficient depends upon the material characteristics of the respective semiconductor. For example, the high refractive index of a semiconductor such as GaAs, (n = 3.3), causes that light incident on the surface of an epitaxial layer structure is refracted towards the normal (n = 3.3), causes that light incident on the surface of an epitaxial layer structure is refracted towards the normal for example, and away from the required orientation. Efficient coupling of the intersubband transition can be achieved by a number of optical techniques, including the use of a beveled edged device, diffraction gratings, and combined diffraction gratings and waveguides.[3]

In addition to absorption, it is important to extract the photoexcited carriers out of the quantum well. This is achieved by placing the excited state near the top of the barrier as shown in Figure 2.5. In the case of the bound-to-continuum transition (see Figure a), the excited state is located just above the barriers, while for a bound-to-quasi bound structure (see Figure b) the excited state is just below the barrier. The latter structure provides lower leakage current due to the higher barrier height for the same detection wavelength.

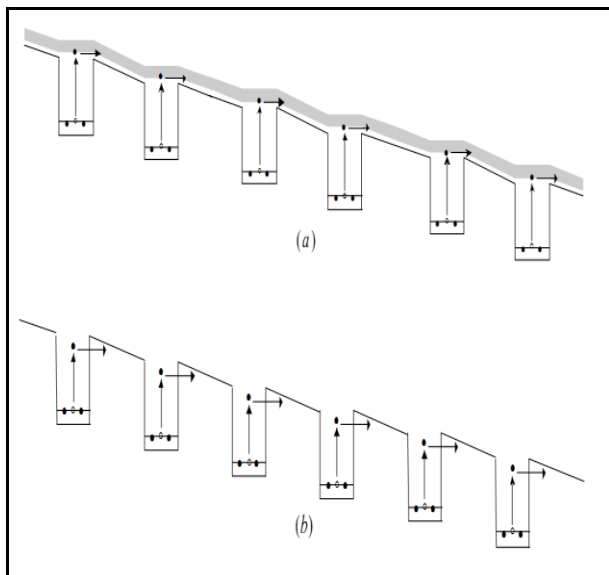


Fig 2.5: Bound-to-continuum (a) and (b) bound-to-bound transitions.

For the bound-to-bound transitions, since there is only one final state, the summation over the initial states in equation gives the number of the electrons in the ground state,

$$N = N_d LA$$

Here,  $N$  is the number of electrons in the initial state,  $N_d$  is the three dimensional doping density, and  $L$  and  $A$  are the well width and area of the quantum structure, respectively. The delta function in Equation is usually replaced by the normalized Lorentzian function to take into account the spectral line width given by:

$$g(\hbar\omega) = \frac{1}{2\pi} \frac{\tau}{(E_f - E_i - \hbar\omega)^2 + (\frac{\tau}{2})^2}$$

Where  $\tau$  is the full width at half the maximum. This is usually obtained experimentally and is about 10-20 meV for intersubband absorption. The transition rate, found using the interaction potential and the momentum operator is given by

$$W_{bound \rightarrow bound} = \frac{N_d (IAL)^2 e^2 \hbar^3}{(\hbar\omega)^2 (m_e^*)^2 \epsilon_0 n_r c} \left| \langle \psi_f | \frac{d}{dz} | \psi_i \rangle \right|^2 g(\hbar\omega)$$

For the bound-to-continuum transitions, the number of initial states is still  $N$  with energy  $E$ , as in the case of bound-to-bound states. However, the summation over the final states requires multiplication by the joint density of states  $r(E)$ , which is defined as:

$$\rho(E) dE = \frac{2dK_z}{(2\pi/l)}$$

For energy states separated by the incident photon energy, the above equation can be reduced to

$$\rho(E) = \frac{l}{2\pi} \sqrt{\frac{2m_b^*}{\hbar^2(E_f - V_b)}}$$

In this expression,  $l$  is the length of the region used for the normalization of the extended state wave function,  $m$  is the electron effective mass in the barrier, and  $V$  is the potential height of the barrier. The transition rate for bound-to-continuum states is then defined as

$$W_{Bound \rightarrow Continuum} = \frac{N_d (IAL)^2 e^2 \hbar^2 l}{2(m_e^*)^2 \epsilon_0 n_r c} \sqrt{\frac{2m_b^*}{(\hbar\omega)^2 (E_f - V_b)}} \left| \langle \psi_f | \frac{d}{dz} | \psi_i \rangle \right|^2$$

This model of the bound to free intersubband absorption is one where the line width is due only to the variation of the joint density of states.[5] The absorption coefficient can be obtained by using both the transition of the matrix element and the transition rate as follows:

$$\alpha(\hbar\omega) = \frac{\text{number of transitions per unit volume and time}}{\text{incident photon flux}} = \frac{W}{I}$$

Thus, the absorption coefficients for the bound-to-bound and bound-to-continuum transitions are given by

$$\alpha_{\text{bound} \rightarrow \text{bound}}(\hbar\omega) = \frac{N_d e^2 \hbar^3}{(\hbar\omega)(m_e^*)^2 \epsilon_0 n_r c} \left| \langle \psi_f | \frac{d}{dz} | \psi_i \rangle \right|^2 g(\hbar\omega)$$

$$\alpha_{\text{bound} \rightarrow \text{continuum}}(\hbar\omega) = \frac{N_d e^2 \hbar^2 l}{2(m_e^*)^2 \epsilon_0 n_r c} \sqrt{\frac{2m_b^*}{(\hbar\omega)^2 (E_f - V_b)}} \left| \langle \psi_f | \frac{d}{dz} | \psi_i \rangle \right|^2$$

The length term,  $l$ , which appears in the bound-to-continuum transition, is eliminated in the normalized final state wave function (assuming it is confined to a length,  $l$ ).

**2.4 Result Analysis:**

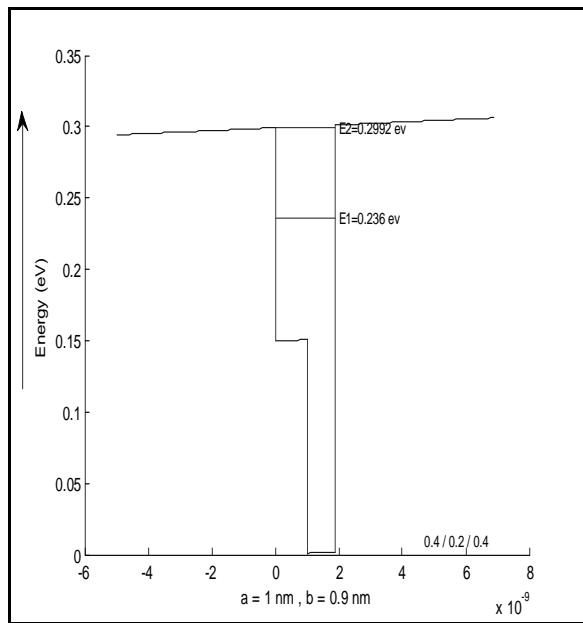


Fig 2.6 Energy levels of AlGaAs / AlGaAs /GaAs/ AlGaAs in quantum potential well.

**Bound-to-bound absorption coefficient for the quantum potential well**

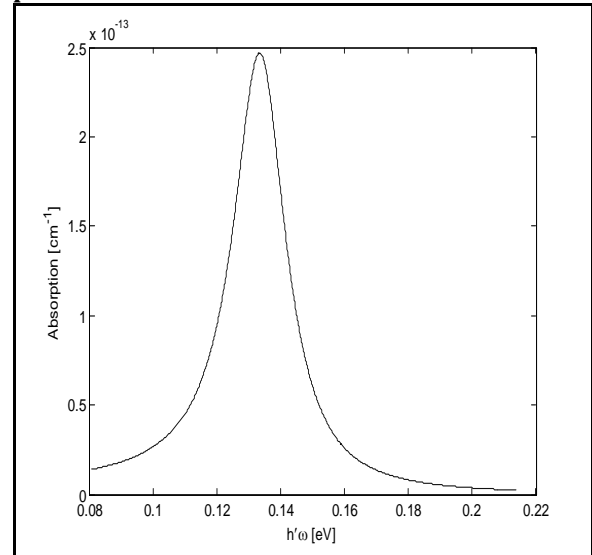


Fig 2.7 Bound-to-bound absorption coefficient for the quantum potential well

Figure 2.7 shows the absorption versus photon energy for bound-to-bound transitions. There is a sharp rise in the absorption spectrum when the photon energy is equal to the difference between the bound state energies in the quantum well structure. The width of the curve depends on the finite lifetime of the excited electron, which was modeled using the Gaussian spectral density function.

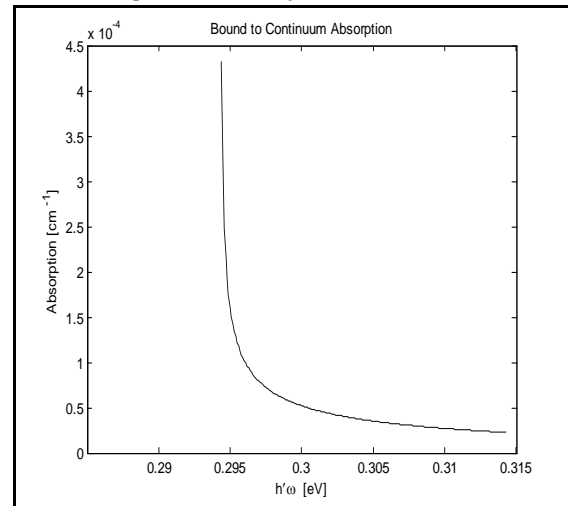


Fig 2.8: Bound-to-continuum absorption coefficient for the quantum well in Figure 2.7 .

Similarly, Figure 2.8 shows the absorption coefficient versus the photon energy for the case of bound-to-continuum transitions. The sharp rise in the spectrum corresponds to a photon energy equal to the difference between the bound state energy and the energy at the top of the quantum well where the extended continuum states begin. As the photon energy increases above this threshold value, absorption increases until reaching a peak value corresponding to the energy above the top of the barrier. At very high energies there is a slow decrease of  $(\hbar\omega)$  since the density of states drops as the energy is increased.[3]

### 2.5 Effect of electric field on quantum wells:

When a uniform electric field is applied along the  $z$  direction (growth direction) the quantum well structure will tilt in the opposite direction of the electric field and the change due to this tilt will affect the energy states of the quantum well. The potential experienced by an electron in the quantum well is given by

$$V(z) = V_n + eFz$$

where  $V_n$  is the potential height of the  $n$ th layer of the quantum well,  $e$  is the electron's charge,  $F$ , measured in  $V/m$ , is the electric field strength, which is applied along the growth direction. A square quantum well in the presence of an external bias is shown in Fig 2.9

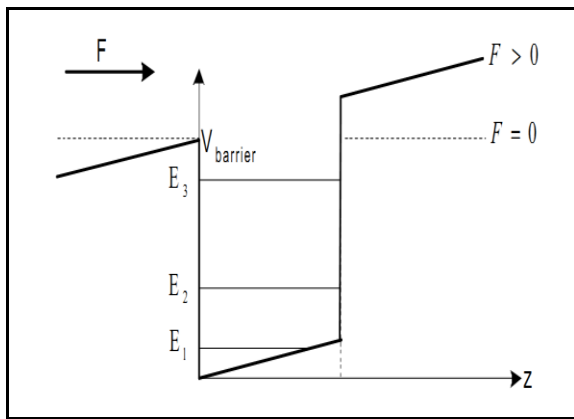


Fig 2.9: Schematic representation of a square quantum well under an applied bias

By increasing the electric field, the lowest energy state  $E_1$  in the quantum well will decrease in energy and fall into to the triangular potential formed at the bottom of the well. On the other hand, the excited states are less affected by the external electric field. However, for low electric field strengths, the

shifting of all the energy levels are the same due to the symmetry of the square well. This can be altered using an asymmetric quantum well, which is equivalent to a square well under a high electric field.

### Transfer Matrix Approach for Quantum Wells Under Applied Bias

We have already discussed the calculation of the energy levels and wavefunctions of arbitrary quantum wells using transfer matrix approach. However, this particular approach cannot be used directly due to the linear variation of the potential energy under an external bias.

One way to overcome this problem is to approximate the linear potential due to the bias with a series of steps or "staircase" as shown in Figure 2.11. The advantage of this approach compared to the use of Airy functions is that, it can be used at The Schrödinger equation for an electron in the quantum well in the presence of an electric field  $F$  can be written as

$$-\frac{\hbar^2}{2m_n^*} \frac{d^2}{dz^2} \psi_n - (E - V_n - qFz) \psi_n = 0$$

where  $E$  is the energy of the electron in the layer and  $V_n$  and  $m_n^*$  are the potential and the effective mass in the  $n$ th layer, respectively. In order to apply the transfer matrix relations it is necessary to know the boundary conditions at the end points. For bound states, we can use the same approach as used in the zero bias case. For the continuum states we can assume that the electron is incident from the left side of the potential shown in

Fig 2.10, and which gives  $B_n=0$ . Thus, starting from  $\frac{A_1}{B_1}$  all the

unknown  $\frac{A_n}{B_n}$  coefficients can be progressively calculated, ending

with the coefficient  $\frac{A_n}{0}$ . Therefore the electron wave

functions can easily be obtained because all the coefficients are produced when  $A_1$  is known (Hutchings, 1989).

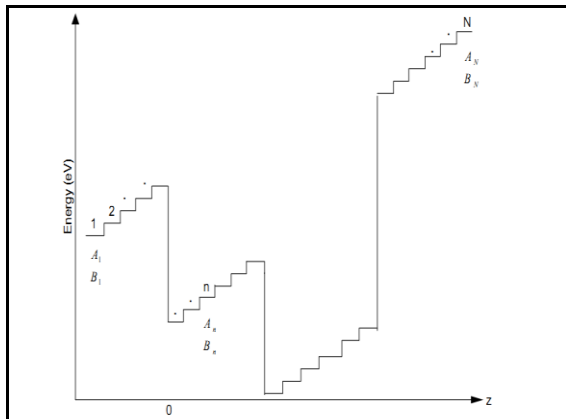


Fig 2.10: The stair case approximation of the potential

**2.5.1 Result Analysis:**

The strength of absorption is found to increase with increasing electric field, mainly due to the stronger matrix element. The asymmetry observed between positive and negative biases is due to the fact that under forward bias (negative), the first excited energy level moves toward the ground state and hence the transition energy is reduced, while under reverse bias (positive) the opposite is true and the transition energy is increased. The mechanisms for Electroabsorption modulator are Franz-Keldysh effect and Quantum-confined Stark effect [2]. Both of these electroabsorption effects are prominent near the bandgap of semiconductors. In case of Stark Effect, Excitonic effects gives rise to a step-like rise in absorption spectra. Formation of excitons manifests themselves as a series of sharp resonances near the bandgap energy. The above result shows a sharp step-like rise in absorption spectra.

**Effect of electric field on the bound state energies of a step quantum for the field strength:**

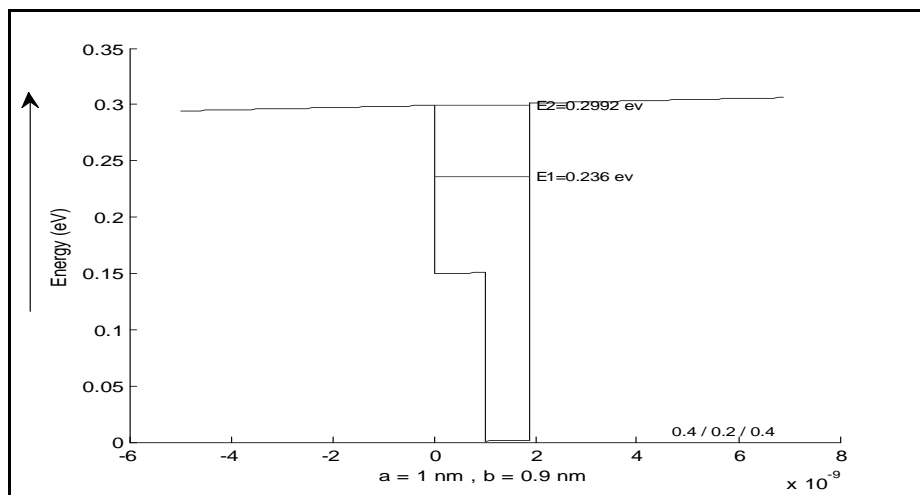


Figure 2.11 Effect of electric field on the bound state energies of a step quantum we for the following field strengths: F=0

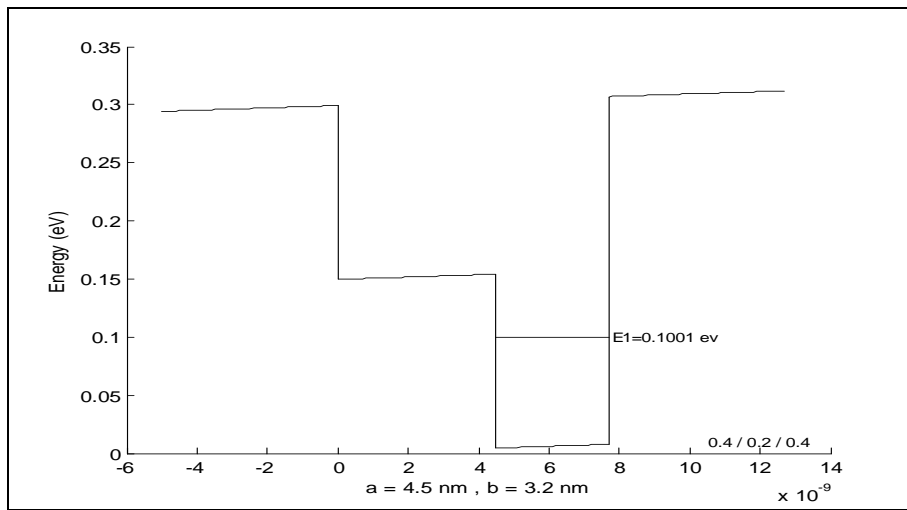


Figure 2.12 Effect of electric field on the bound state energies of a step quantum we for the following field strengths:  $F = 1\text{mV/m}$

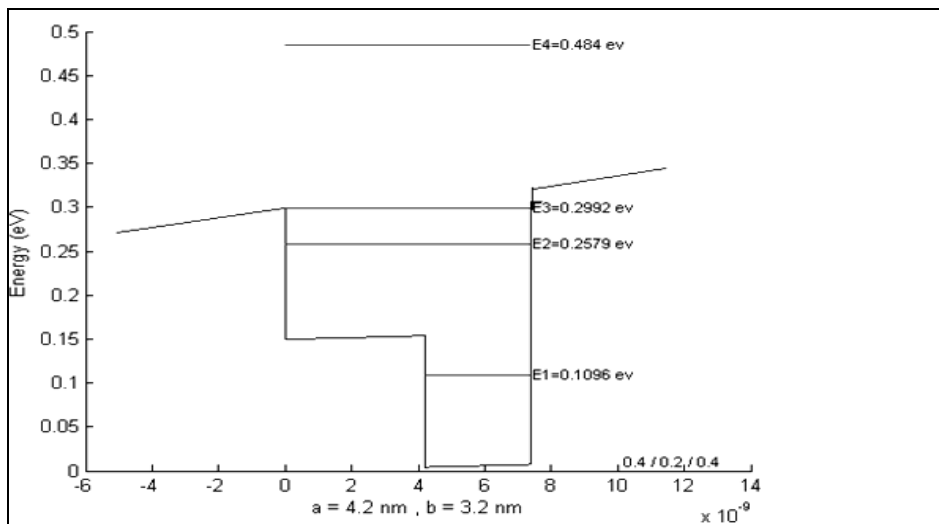
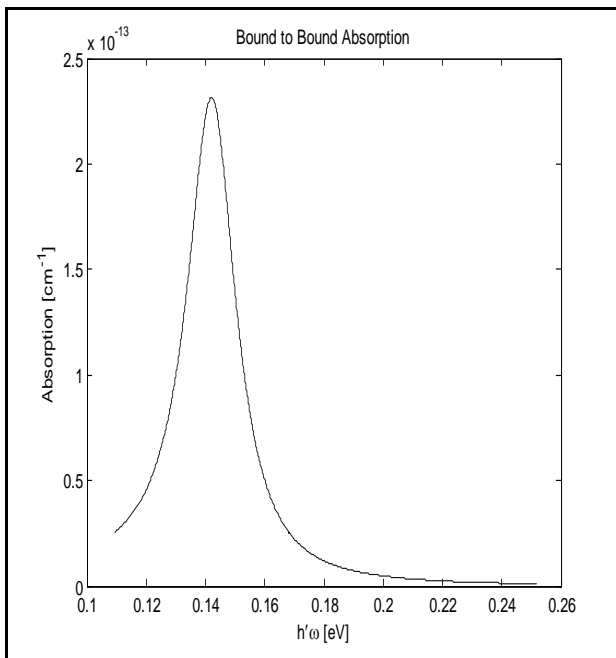
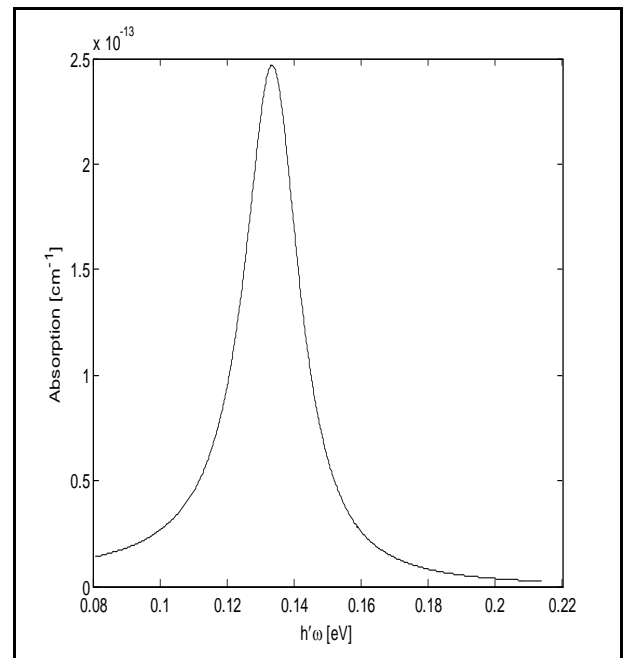


Figure 2.13 Effect of electric field on the bound state energies of a step quantum for the field strengths  $F = 10\text{mV/m}$ .

**Intersubband Absorption Under an Applied Electric Field**



a)calculated absorption coefficient as a function of bias across the well,bias=1V/μm



b)calculated absorption coefficient as a function of bias across the well,bias=10V/μm

Fig 2.14 Calculated absorption coefficient as a function of bias

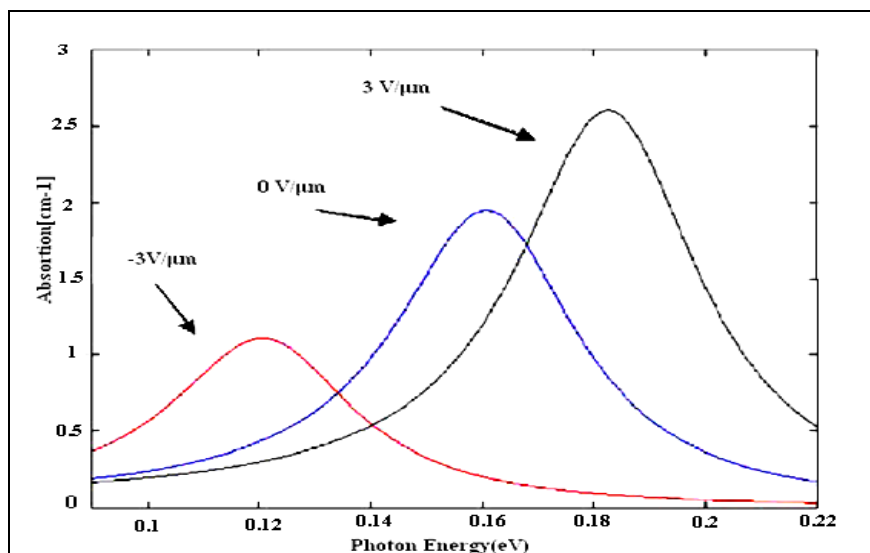


Fig 2.15:the calculated absorption coefficient as a function of bias across the well



## Conclusion:

An attempt has been made design a Step Asymmetric Quantum well with AlGaAs /GaAs/ AlGaAs material. We derive the expression of absorption coefficient which is important in the development of Tunable Photo Detector and Electro-Absorption Modulator. Thereby, graphs are plotted with absorption co-efficient as a function of external bias across the well. So, this is similar to the mechanisms of Photo Detector and Electro-Absorption Modulator. The mechanisms for Electroabsorption modulator are Franz-Keldysh effect and Quantum-confined Stark effect. Both of these electro absorption effects are prominent near the bandgap of semiconductors. In case of Stark Effect, Excitonic effects gives rise to a step-like rise in absorption spectra. Formation of excitons manifests themselves as a series of sharp resonances near the bandgap energy. The above result shows a sharp step-like rise in absorption spectra. The electro absorption optical modulator (EA modulator) is an optical modulator that utilizes the electroabsorption effect that the optical Absorption Coefficient of a substance varies depending on the electric field applied to it. The EA modulator is generally classified into a type using absorption Waveguide Layer having a quantum well structure and a type using a bulk Semiconductor layer rather than a waveguide layer. Variable optical attenuators (VOA) are used to permit dynamic control of Optical Power levels throughout a communications, telecommunications or other transmission network. As traffic in networks increase. VOAs may be used to dynamically lower the optical power levels depending on the length of the Network route so that appropriate power levels are received at the end receivers. The performance of optical modulators may be affected by numerous factors, such as a change in the environmental temperature.

For modulators in telecommunications small size and modulation voltages are desired. The EAM is candidate for use in external modulation links in telecommunications. These modulators can be realized using either bulk semiconductor materials or materials with multiple quantum dots or wells.

Semiconductor quantum well EAM is widely used to modulate near-infrared (NIR) radiation at frequencies below 0.1THz. Allows a single optical power source to be used for large number of information carrying beams.

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