

# Analytical Study of Algorithms for Mining Association Rules from Probabilistic Databases and future possibilities

Niket Bhargava<sup>1</sup>, Dr. Manoj Shukla<sup>2</sup>

<sup>1</sup>Department of Comp. Sc. & Engg., Mewar University, India

<sup>2</sup>Professor, Department of E&C, BCE, Mandideep, Bhopal, India

**Abstract** — we consider the problem of discovering frequent item sets and association rules between items in a large database of transactional databases acquired under uncertainty. With each transaction associated is a probability gives the confidence that the transaction will occur. We discuss generalized algorithms for solving this problem that are fundamentally different from the known algorithms. Complete demonstration of algorithm presented and discussed in this paper. We also show how the best features of the algorithm can be combined into a business system.

**Keywords:** Data Mining, Big Data, Data Science, Association Rule Mining, Probabilistic frequent patterns, probabilistic frequent rule.

## 1. INTRODUCTION

Now a days business databases not only recording exact transactions but at the same time also recording instable business circumstances into the data and hence with each and every possible transaction are associating a confidence or probability value that indicates strength by which the transaction will took place in real business world. Field of analytics specially predictive and prescriptive analytics playing critical role and are of great use to motivate probabilistic databases. Progress in digital bar-coding technology has made it possible for organizations to collect and store massive amounts of sales data, referred to as the basket data. A record in such data typically consists of the transaction date and the items bought in the transaction. Successful organizations view such databases as important pieces of the marketing infrastructure. They are interested in instituting information-driven marketing processes, managed by database technology, that enable marketers to develop and implement customized marketing programs and strategies [6].

The problem of mining association rules over market basket data was introduced in [4]. An example of such a rule might be that 98% of customers that purchase tires and auto accessories also get automotive services done. Finding all such rules is valuable for cross-marketing, cross-sell, up-sell, targeted marketing, product bundling and propensity focused attached mailing applications. Other applications

include catalog design, add-on sales, store layout, and customer segmentation based on buying patterns. The databases involved in these applications are very large. It is imperative, therefore, to have fast algorithms for this task[23].

The following is a formal statement of the problem [4]: Let  $I = \{i_1, i_2, \dots, i_m\}$  be a set of literals, called items. Let  $D$  be a set of transactions, where each transaction  $T$  is a set of items such that  $T \subseteq I$ . Associated with each transaction is a unique identifier, called its TID. We say that a transaction  $T$  contains  $X$ , a set of some items in  $I$ , if  $X \subseteq T$ . An association rule is an implication of the form  $X \Rightarrow Y$ , where  $X \subset I$ ,  $Y \subset I$ , and  $X \cap Y = \emptyset$ . The rule  $X \Rightarrow Y$  holds in the transaction set  $D$  with confidence  $c$  if  $c\%$  of transactions in  $D$  that contain  $X$  also contain  $Y$ . The rule  $X \Rightarrow Y$  has support  $s$  in the transaction set  $D$  if  $s\%$  of transactions in  $D$  contain  $X \cup Y$ . Our rules are somewhat more general than in [4] in that we allow a consequent to have more than one item[23]. Given a set of transactions  $D$ , the problem of mining association rules is to generate all association rules that have support and confidence greater than the user specified minimum support (called minsup) and minimum confidence (called minconf) respectively. Our discussion is neutral with respect to the representation of Database  $D$ . For example,  $D$  could be a data file, a relational table, or the result of a relational expression[23]. An algorithm for finding all association rules, henceforth referred to as the AIS algorithm, was presented in [4]. Another algorithm for this task, called the SETM algorithm, has been proposed in [13]. In this paper, we restudied algorithms, Apriori and Probabilistic\_Apriori, that differ fundamentally from these algorithms.

The problem of finding frequent item sets and association rules falls within the purview of database mining [3] [12], also called knowledge discovery in databases [21]. Related, but not directly applicable, work includes the induction of classification rules [8] [11] [22], discovery of causal rules [19], learning of logical definitions [18], fitting of functions to data [15], and clustering [9] [10]. The closest work in the machine learning literature is the KID3 algorithm presented

in [20]. If used for finding all association rules, this algorithm will make as many passes over the data as the number of combinations of items in the antecedent, which is exponentially large. Related work in the database literature is the work on inferring functional dependencies from data [16]. Functional dependencies are rules requiring strict satisfaction. Consequently, having determined a dependency  $X \rightarrow A$ , the algorithms in [16] consider any other dependency of the form  $X + Y \rightarrow A$  redundant and do not generate it. The association rules we consider are probabilistic in nature. The presence of a rule  $X \rightarrow A$  does not necessarily mean that  $X + Y \rightarrow A$  also holds because the latter may not have minimum support. Similarly, the presence of rules  $X \rightarrow Y$  and  $Y \rightarrow Z$  does not necessarily mean that  $X \rightarrow Z$  holds because the latter may not have minimum confidence. There has been work on quantifying the “usefulness” or “interestingness” of a rule [20]. What is useful or interesting is often application-dependent. The need for a human in the loop and providing tools to allow human guidance of the rule discovery process has been articulated, for example, in [7] [14].

Original Apriori works on exact non-probabilistic transactions. But transactions in real world occur with some uncertain probability. Data uncertainty is inherent in applications such as sensor monitoring systems, location-based services, and biological databases. To record and manage this vast amount of imprecise, uncertain information, probabilistic databases have been recently developed. In this paper, we study the discovery of frequent patterns and association rules from probabilistic databases under the Possible World Semantics. This is technically challenging, since a probabilistic database can have an exponential number of possible worlds. We evaluated probabilistic apriori algorithms, which discover frequent patterns in bottom-up manner likewise Apriori.

## 1.2 Problem Decomposition and Paper Organization

In case of non-probabilistic databases the problem of discovering all association rules can be decomposed into two subproblems[4]:

(1). Find all sets of items (itemsets) that have transaction support above minimum support. The support for an itemset is the number of transactions that contain the itemset. Itemsets with minimum support are called large itemsets, and all others small itemsets.

(2). Use the large itemsets to generate the desired rules. Here is a straightforward algorithm for this task. For every large itemset  $l$ , and all non-empty subsets of  $l$ . For every such subset  $a$ , output a rule of the form  $a \Rightarrow (l - a)$  if the ratio of

support( $l$ ) to support( $a$ ) is at least minconf. We need to consider all subsets of  $l$  to generate rules with multiple consequents. Due to lack of space, we do not discuss this subproblem further, but refer the reader to [5] for a fast algorithm.

## 1.3 Discovering Large Itemsets

Algorithms for discovering large itemsets make multiple passes over the data. In the first pass, we count the support of individual items and determine which of them are large, i.e. have minimum support. In each subsequent pass, we start with a seed set of itemsets found to be large in the previous pass. We use this seed set for generating new potentially large itemsets, called candidate itemsets, and count the actual support for these candidate itemsets during the pass over the data. At the end of the pass, we determine which of the candidate itemsets are actually large, and they become the seed for the next pass. This process continues until no new large itemsets are found. The Apriori and AprioriTid algorithms differ fundamentally from the AIS[4] and SETM[13] algorithms in terms of which candidate itemsets are counted in a pass and in the way that those candidates are generated. In both the AIS and SETM algorithms, candidate itemsets are generated on-the-fly during the pass as data is being read. Specifically, after reading a transaction, it is determined which of the itemsets found large in the previous pass are present in the transaction. New candidate itemsets are generated by extending these large itemsets with other items in the transaction. However, the disadvantage with the Apriori and AprioriTID algorithms is that they generate the candidate itemsets to be counted in a pass by using only the itemsets found large in the previous pass. The basic intuition is that any subset of a large itemset must be large. Therefore, the candidate itemsets having  $k$  items can be generated by joining large itemsets having  $k-1$  items, and deleting those that contain any subset that is not large. This procedure results in generation of a much smaller number of candidate itemsets. Apriori is explained in next section 2, than in section 3 problem of finding probabilistic frequent itemset is defined and in section 4 problem is solved fully on toy database.

## 2 APRIORI ALGORITHM

In this section we will revisit Apriori algorithm. Notation We assume that items in each transaction are kept sorted in their lexicographic order. It is straightforward to adapt these algorithms to the case where the database DB is kept normalized and each given database record is a  $\langle TID, item \rangle$

pair, where TID is the identifier of the corresponding transaction. We call the number of items in an itemset its size, and call an itemset of size  $k$  a  $k$ -itemset. Items within an itemset are kept in lexicographic order. We use the notation  $c[1].c[2]. \dots c[k]$  to represent a  $k$ -itemset  $c$  consisting of items  $c[1], c[2], \dots, c[k]$ , where  $c[1] < c[2] < \dots < c[k]$ . if  $c$  is  $XY$  is an  $m$ -itemset, we also call  $Y$  an  $m$ -extension of  $X$ . Associated with each itemset is a count field to store the support for this itemset. The count field is initialized to zero when the itemset is first created. We summarize in table 1 the notation used in the algorithms.

**TABLE -1: NOTATIONS FOR APRIORI**

k-itemset	An itemset having k items.
$L_k$	Set of large $k$ -itemsets $L_k$ #those with minimum support#. Each member of this set has two fields: $i$ # itemset and $ii$ # support count.
$C_k$	Set of candidate $k$ -itemsets $C_k$ #potentially large itemsets#. Each member of this set has two fields: $i$ # itemset and $ii$ # support count.

**2.1 Algorithm Apriori**

Figure 1 gives the Apriori algorithm. The first pass of the algorithm simply counts item occurrences to determine the large 1-itemsets. A subsequent pass, say pass  $k$ , consists of two phases. First, the large itemsets  $L_{k-1}$  found in the  $(k-1)$ th pass are used to generate the candidate itemsets  $C_k$ , using the apriori gen function described in 2.1.1. Next the database is scanned and the support of candidates in  $C_k$  is counted. For fast counting, we need to efficiently determine candidates in  $C_k$  that are contained in a given transaction  $t$ . See [5] for a discussion of buffer management.

- 1)  $L_1 = \{ \text{large 1-itemsets} \};$
- 2) for (  $k = 2; L_{k-1} \neq \Phi; k++$  ) do begin
- 3)  $C_k = \text{apriori-gen}(L_{k-1});$  // New candidates
- 4) forall transactions  $t \in D$  do begin
- 5)  $C_t = \text{subset}(C_k, t);$  // Candidates contained in  $t$
- 6) forall candidates  $c \in C_t$  do
- 7)  $c.\text{count}++;$
- 8) end
- 9)  $L_k = \{ c \in C_k \mid c.\text{count} \geq \text{minsup} \}$
- 10) end
- 11) Answer =  $\cup_k L_k;$

**Figure -1: Algorithm Apriori**

**2.2 The apriori-gen function**

The apriori-gen function takes as argument  $L_{k-1}$ , the set of all large  $(k-1)$ -itemsets. It returns a superset of the set of all large  $k$ -itemsets. The function works as follows. 1 First, in the join step, we join  $L_{k-1}$  with  $L_{k-1}$ :

the logic implemented using sql query form is as follows;

```
(1) insert into C_k
select p.item[1], p.item[2], ..., p.item[k-1], q.item[k-1]
from L_{k-1} p, L_{k-1} q
where p.item[1] = q.item[1], ..., p.item[k-2] = q.item[k-2], p.item[k-1] < q.item[k-1];
```

Next, in the prune step, we delete all itemsets  $c \in C_k$  itemsets such that some  $(k-1)$ -subset of  $c$  is not in  $L_{k-1}$

```
(1) forall itemsets c ∈ C_k do
    forall (k-1)-subsets s of c do
        if ( c not belongs to L[k-1] ) then
            delete c from C_k;
```

**3. Probabilistic FREQUENT PATTERN AND ASSOCIATION RULE MINING**

In this section we will discuss mining uncertain database data with probabilistic certainty. Data uncertainty is inherent in many applications such as sensor monitoring systems, location-based services, and biological databases. To manage this vast amount of imprecise information, probabilistic databases have been recently developed. In this paper, we study the discovery of frequent patterns and association rules from probabilistic data under the Possible World Semantics. This is technically challenging, since a probabilistic database can have an exponential number of possible worlds. The data managed in many emerging applications is often uncertain. Integration and record linkage tools, for example, associate confidence values to the output tuples according to the quality of matching [34]. In structured information extractors, confidence values are appended to rules for extracting patterns from unstructured data [52]. In habitat monitoring systems, data collected from sensors like temperature and humidity are noisy [34]. The locations of users obtained through RFID and GPS systems are also imprecise [25, 39]. To handle these problems, probabilistic databases have been recently proposed, where uncertainty is treated as a “first-class citizen” [31, 34, 44, 33, 38]. Due to its simplicity in database design and query semantics, the *tuple-uncertainty* model is commonly used in probabilistic databases. Conceptually, each tuple carries an *existential probability* attribute, which denotes the confidence that the tuple exists. Figure 2 illustrates this model, which records traffic violation events due to red-light running. The details of each event (e.g., location, and traffic volume) are captured by a red-light camera system, which contains sensors and cameras mounted in road intersections. Each tuple is annotated by a probability that a true violation happens. The probability that a violation occurs is determined by sensor measurement errors, as well as the uncertainty caused by automatic information extraction of the photographs taken by the system [53].

ID	location	time	speed	traffic	weather	prob
t1	x	8-	30-40	high	Rain	0.1
t2	x	7-	80-90	low	null	1.0
t3	x	8-	80-90	low	Foggy	0.5
t4	x	8-	30-40	high	Rain	0.2
t5	y	2-	50-60	low	Sunny	1.0

Figure -2: A probabilistic database example

To interpret tuple uncertainty, the Possible World Semantics (or PWS in short) is often used [34]. Conceptually, a database is viewed as a set of deterministic instances (called possible worlds), each of which contains a set of zero or more tuples. A possible world for Figure 2 consists of the tuples { t2, t3, t5 }, existing with a probability of  $(1 - 0.1) \times 1.0 \times 0.5 \times (1 - 0.2) \times 1.0 = 0.036$ . Any query evaluation algorithm for probabilistic database has to be correct under PWS. That is, the results produced by the algorithm should be the same as if the query is evaluated on every possible world [34]. Although PWS is intuitive and useful, evaluating queries under this notion is costly. This is because a probabilistic database has an exponential number of possible worlds. For example, the table in Figure 1 has  $2^3 = 8$  possible worlds. Performing query evaluation or data mining under PWS can thus be technically challenging. In fact, the mining of uncertain or probabilistic data has recently attracted research attention [26]. In [41], efficient clustering algorithms were developed to group uncertain objects that are close to each other. Recently, a Naive Bayes classifier has been developed [49]. The goals of this paper are: (1) propose a definition of frequent patterns and association rules for the tuple uncertainty model; and (2) develop efficient algorithm for mining frequent patterns and association rules.

Association rule	Probability
r1: {location=x} $\Rightarrow$ {time=8-9pm}	0.15
r2: {location=x} $\Rightarrow$ {speed=80-90, traffic=low}	0.49

Figure -3: Sample p-ARs derived from Figure 2

The frequent patterns discovered from probabilistic data are also probabilistic, to reflect the confidence placed on the mining results. Figure 3 shows two probabilistic frequent patterns (or p-FP) extracted from the database in Figure 2. A p-FP is a set of attribute values that occur frequently with sufficiently high probabilities. The pmf of the number of tuples is the support count that contains a pattern with specific probability. Under PWS, a database is a set of possible worlds, each of which records a (different) support of the same pattern. Hence, the support of a frequent pattern is a pmf. In figure 1, if we consider all possible worlds where { location = x } occurs three times, the pmf of { location

= x } with a support of 3 is 0.49. for the p-FP shown. Figure 3 displays their related probabilistic association rules (or p-ARs). Here, rule r2 suggests that with a 0.49 probability, 1) red-light violations occur frequently at location x and 2) when this happens, the involved vehicle is likely driving at a high speed amid low traffic. We will later explain more about the semantics of p-FP and p-AR. A simple way of finding p-FPs is to extract frequent patterns from every possible world. This is practically infeasible, since the number of possible worlds is exponentially large.

**Prior work.** [30] studied approximate frequent patterns on noisy data, while [42] examined association rules on fuzzy sets. The notion of a “vague association rule” was developed in [43]. These solutions were not developed on probabilistic data models. For probabilistic databases, [32, 25] derived patterns based on their expected support counts. [54, 50] found that the use of expected support may render important patterns missing. They discussed the computation of the probability that a pattern is frequent. While [55] handled the mining of *single* items, our solution can discover patterns with more than one item. The data model used in [50] assumes that for each tuple, each attribute value has a probability of being correct. This is different from the tuple-uncertainty model, which describes the joint probability of attribute values within a tuple. pmf evaluation method DC algorithm is asymptotically faster than the DP algorithms used in [54, 50], and is thus more scalable for large and dense datasets. To our best knowledge, none of the above works considered the important problem of generating association rules on probabilistic databases.

This section is organized as follows. Section 3.1 introduces the notions of p-FPs and p-ARs. Sections 3.2 present our algorithms for mining p-FPs. Section 3.3 discusses fully solved example using dataset used in paper introduced Pascal algorithm. The CIPFP algorithm is described in section 5 and example is described in section 6

### 3.1 Problem Definition

We first review frequent patterns and association rules in Sections 3.1.1. Then, we discuss the uncertain data model in Section 3.1.2. We present the problems of mining p-FPs and p-ARs, in Sections 3.1.3 and 3.1.4.

#### 3.1.1 Frequent Patterns and Association Rules

A transaction is a set of items (e.g., goods bought by a customer in a supermarket). A set of items is also called an itemset or a pattern. Given a transaction database of size n and a pattern X, we use sup(X) to denote the support of X, i.e., the number of times that X appears in the database. A pattern X is frequent if:

$$\text{sup}(X) \geq \text{minsup} \tag{1}$$

where  $\text{minsup} \in N \cap [1, n]$  is the support threshold [27].

Given patterns  $X$  and  $Y$  (with  $X \cap Y = \emptyset$ ), if pattern  $XY$  is frequent, then  $X$  is also frequent (called the anti-monotonicity property). Also,  $X \Rightarrow Y$  is an association rule if following conditions holds:

$$\text{supp}(XY) \geq \text{minsup} \tag{2}$$

$$\text{supp}(XY)/\text{supp}(X) \geq \text{minconf} \tag{3}$$

$\text{sup}(XY) / \text{sup}(X)$ , denoted by  $\text{conf}(X \Rightarrow Y)$ , is the confidence of  $X \Rightarrow Y$ , and  $\text{minconf} \in R \cap (0, 1]$  is the confidence threshold. To verify Equation 3, the values of  $\text{sup}(XY)$  and  $\text{sup}(X)$  have to be found first.

We remark that a transaction database is essentially a relational table with asymmetric binary attribute values. For example, the existence of item ‘‘apple’’ in a transaction is equivalent to a binary attribute of a tuple with a value of 1. This kind of attributes, assumed in this paper, is also considered by some mining algorithms (e.g., [27, 28]). To handle other attribute types (e.g., continuous and categorical), discretization and binarization techniques can be used to convert them to binary attributes [52].

### 3.2.2 The Possible World Semantics

We assume that each transaction has an existential probability, which specifies the chance that the transaction exists. Figure 4(a) illustrates this database, in which each transaction is a set of items represented by letters. This model has been used to capture uncertainty in many applications, including data streams[33] and geographical services[45]. Now, let  $P(E)$  be the probability that an event  $E$  occurs and PDB be probabilistic database of size  $n$ . Also, let  $T_i$  (where  $i = 1, \dots, n$ ) be the ID of each tuple in PDB. Suppose  $T_i.S$  is the set of items contained in  $T_i$ , and  $T_i.p$  is the existential probability of  $T_i$ .

ID	SetOfItems	Probability/confidence
T 1	{a, c, e, g, i}	0.6
T 2	{a, c, f, h}	0.5
T 3	{a, d, e, g, j}	0.7
T 4	{b, d, f, h, i}	1.0

Figure -4(a): A probabilistic database

Under PWS, PDB is a set of possible worlds  $W$ . Figure 4(b) lists all possible worlds for figure 4(a). Each  $W_i \in W$  exists with probability  $P(W_i)$ . For example  $P(W_2) = T1.p \times (1 - T2.p) \times (1 - T3.p) \times T4.p$  or 0.09. The sum of possible world probabilities is one. Also, the number of possible worlds is exponentially large,

i.e.  $|w| = O(2^n)$ . Our goal is to discover patterns and rule using these possible worlds.

W	Tuples in W	Prob.	W	Tuples in W	Prob.
W1	T4	0.06	W5	T1, T2, T4	0.09
W2	T1, T4	0.09	W6	T1, T3, T4	0.21
W3	T2, T4	0.06	W7	T2, T3, T4	0.14
W4	T3, T4	0.14	W8	T1, T2, T3, T4	0.21

Figure -4(b):Possible World for PDB in Figure 4(a)

### 3.2 Probabilistic Frequent Patterns

we first explain the concept of support for probabilistic data. Given a pattern  $X$ , we denote its support in each world  $W_i$  as  $\text{sup}_i(X)$  is obtained by counting the number of times  $X$  appears in  $W_i$ . Since each  $W_i$  exists with a probability, the support of  $X$  in PDB, i.e.  $\text{sup}(X)$ , is a random variable. We denote  $f_x(k)$  that the probability mass function (pmf) of  $\text{sup}(X)$  can take. Specifically,  $f_x(k)$  is the probability that  $\text{sup}(X) = k$ , and  $f_x(k) = 0$  for any  $k \notin [0, n]$ . We use an array to store the non-zero values of  $f_x$ , where  $f_x[k] = P(\text{sup}(X) = k)$ . Figure 4(c) depicts the support pmf of  $\{a\}$ . the probability that  $\text{sup}(\{a\}) = 1$  is 0.29.

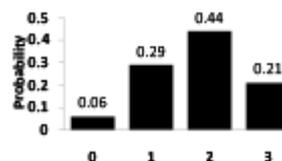


Figure -4(C): Support pmf for 1-itemset {a} in PWS

### DEFINITION 1. A pattern $X$ is a

probabilistic frequent pattern or p-FP in PDB if  $P(\text{sup}(X) \geq \text{minsup}) \geq \text{minprob}$  (4) where  $\text{minprob} \in R \cap (0, 1]$  is the probability threshold.

**Problem 1 (p-FP Mining).** Given PDB,  $\text{minsup}$  and  $\text{minprob}$ , return a set of  $\{X, f_x(k)\}$ , where  $X$  is a p-FP. As we will discuss, the pmfs obtained with p-FPs are essential to generating probabilistic association rules. There are methods to approximating and compressing pmfs (e.g., see [35]). Here we assume that the pmf is exact, but our solutions can be extended to support these schemes. Next, we present a useful lemma.

**Lemma 1 (Anti-monotonicity).** If pattern  $X$  is a p-FP, then any pattern  $X' \subset X$  is also a p-FP.

The anti-monotonicity property is true for frequent patterns in exact data [27]. Lemma 1 allows us to stop examining a pattern, if any of its sub-pattern is not a p-FP. A p-FP  $X$  is said to be maximal if we cannot find another p-

FP Y such that  $X \subset Y$ . A maximal p-FP can succinctly represent a set of p-FPs when their supports are not concerned. Since the mining of maximal frequent patterns is an important problem [28] for exact data, we also study maximal p-FPs, together with free set, maximal set make a complete system, we study them too;

**Problem 2.1 (Free set p-FP Mining).** Given a database PDB, minsup and minprob, return all minimal generators or free sets p-Fps.

**Problem 2.2 (Maximal p-FP Mining).** Given a database PDB, minsup and minprob, return all maximal p-Fps.

**Problem 2.3 (closed p-FP Mining).** Given a database PDB, minsup and minprob, return all closed p-FPs.

### 3.3 Probabilistic Association Rules

In a probabilistic database, the support counts of patterns are random variables. Let  $P(X \Rightarrow Y)$  be the probability that  $X \Rightarrow Y$  is an association rule. By Equations 2 and 3, we have:

$$P(X \Rightarrow Y) =$$

$$P[\text{sup}(XY) > \text{minsup} \wedge \text{conf}(X \Rightarrow Y) \geq \text{minconf}] \quad (5)$$

**Definition 2.**  $X \Rightarrow Y$  is a probabilistic association rule

(p-AR in short) if

$$P(X \Rightarrow Y) \geq \text{minprob} \quad (6)$$

The problem of p-AR mining is defined as follows.

**Problem 3 (p-AR Mining).** Given minsup, minprob, minconf, and the p-FPs and their support pmfs obtained from Problem 1, derive all p-ARs and their probabilities.

A simple way of solving Problems 1, 2, and 3 is to expand PDB into all possible worlds, compute patterns and rules from each world, and then combine the results. If minsup=2, minconf=0.5, and minprob=0.2, for Figure 4(a),  $\{a\} \Rightarrow \{c\}$  is an association rule only in worlds W5 and W8 (Figure 4(c)), with  $P(\{a\} \Rightarrow \{c\}) = \text{Pr}(W5) + \text{Pr}(W8) = 0.09 + 0.21 = 0.3$ . Since this is larger than 0.2,  $\{a\} \Rightarrow \{c\}$  is a p-AR. This method is not practical, due to the large number of possible worlds. To tackle Problems 1 and 2, proposed algorithms, namely probabilistic Apriori discussed and solved fully in next section 4.

#### 4. Probabilistic Apriori using PWS fully Solved case

In this section we display the probabilistic Apriori using PWS fully Solved using toy database used in research paper by Bastides et. al. described algorithm Pascal. To solve Problem 1, we discussed the probabilistic-Apriori algorithm, which is an adaptation of the Apriori algorithm [27] for probabilistic databases. Specifically, probabilistic-Apriori uses the bottom-up framework [27]: using PWS.

##### 4.1 Our Probabilistic Algorithm: Probabilistic Apriori

1. PDB Database making,
2. PWS making using PDB,
3. Define candidate  $C_1$  1-itemset equal to Item Collection I.
4. PDB database scan for all c belongs to  $C_1$  to calculate support c.support. Store them in a list call it FP.

5. PWS database scan for all c in FP and all c.support where support is equal to "0" to "c.support" to evaluate  $fc[k]$  probability pmf support.

6. Determining Probabilistic Frequent Patterns using minsup and minprob. First compare minsup with c.support. If c.support  $\geq$  minsup than using pmf for pattern c in  $C_1$  compare  $fc[k] \geq$  minprob. Collect all c in PFP and assign it to  $L_1$  all along with valid frequent probable support and probability. Call it  $L_1$ .

7.1)  $L_1 = \{ \text{large 1-itemsets} \};$

7.2) for (  $k = 2; L_{k-1} \neq \Phi; k++$  ) do begin

7.3)  $C_k = \text{apriori-gen}(L_{k-1});$  // New candidates

7.4) forall transactions  $t \in$  PDB do begin

7.5)  $C_t = \text{subset}(C_k, t);$  // Candidates contained in t

7.6) forall candidates  $c \in C_t$  do

7.7) c.count++;

7.8) end

7.9)  $FP = \{ c \in C_k \mid c.\text{count} \geq \text{minsup} \}$

7.10) forall fp  $\in$  FP

7.11) from  $k = 0$  to fp.support

7.12)  $W = w \in$  PWS exactly with size k times k number of transactions

7.13)  $Ffp[k].\text{prob}++;$

7.14) end

7.15)  $PFP = \{ FP \in FP_k \mid Ffp[k].\text{prob} \geq \text{minprob} \}$

7.15)  $L_k = PFP$

7.16) end

7.17) Answer =  $\cup_k L_k;$

**Figure -5:** Probabilistic Apriori Algorithm

##### A. The apriori-gen function

The apriori-gen function takes as argument  $L_{k-1}$ , the set of all large (k-1)-itemsets. It returns a superset of the set of all large k-itemsets. The function works as follows. 1 First, in the join step, we join  $L_{k-1}$  with  $L_{k-1}$ : the logic is in the form of sql query form is as follows;

```
(1) insert into  $C_k$ 
    select p.item[1], p.item[2], ..., p.item[k-1], q.item[k-1]
    from  $L_{k-1}$  p,  $L_{k-1}$  q
    where p.item[1] = q.item[1], ..., p.item[k-2] =
    q.item[k-2], p.item[k-1] < q.item[k-1];
```

Next, in the prune step, we delete all itemsets  $c \in C_k$  itemsets such that some (k-1)-subset of c is not in  $L_{k-1}$ .

(1) forall itemsets  $c \in C_k$  do

forall (k-1)-subsets s of c do  
 if ( c not belongs to  $L_{k-1}$  ) then  
 delete c from  $C_k$  ;

**4.2 Solved Example Probabilistic Apriori**

This section discusses the solved example of probabilistic Apriori on toy database. To explain fully general version is solved to full length. The database used is same as used in paper which presented Pascal Algorithm extended to include the transaction level existential probability and time stamp for time at which transaction took place. Figure 6 depicts Pascal Transaction Temporal Dataset with Probabilistic Confidence. For our Probabilistic Apriori algorithm only column TID, SetOfItems, and Probabilistic/Confidence are of importance or relevant.

TID	SetOfItems	TimeStamp	Key	Probability/Confidence
T1	A, B, C, F	1	?	0.6
T2	B, C, E, F	2	?	0.5
T3	A, B, C, E, F	3	?	0.7
T4	B, E, F	4	?	0.4
T5	A, B, C, E, F	5	?	1.0

Figure -6: PDB for Pascal Transactional Temporal Dataset with Probabilistic Confidence

Using concepts of Possible World Semantics in earlier sections, on database presented in Figure 6 we calculated PWS, which is available in Figure 7.

Worlds	TransactionWorld	WorldProbabilityCalculation	WorldProbability
W1	T5	$(1-0.6)*(1-0.5)*(1-0.7)*(1-0.4)*(1.0)$	0.036
W2	T1T5	$(0.6)*(1-0.5)*(1-0.7)*(1-0.4)*(1.0)$	0.054
W3	T2T5	$(1-0.6)*(0.5)*(1-0.7)*(1-0.4)*(1.0)$	0.036
W4	T3T5	$(1-0.6)*(1-0.5)*(0.7)*(1-0.4)*(1.0)$	0.084
W5	T4T5	$(1-0.6)*(1-0.5)*(1-0.7)*(0.4)*(1.0)$	0.024
W6	T1T2T5	$(0.6)*(0.5)*(1-0.7)*(1-0.4)*(1.0)$	0.054
W7	T1T3T5	$(0.6)*(1-0.5)*(0.7)*(1-0.4)*(1.0)$	0.126
W8	T1T4T5	$(0.6)*(1-0.5)*(1-0.7)*(0.4)*(1.0)$	0.036
W9	T2T3T5	$(1-0.6)*(0.5)*(0.7)*(1-0.4)*(1.0)$	0.084

W10	T2T4T5	$(1-0.6)*(0.5)*(1-0.7)*(0.4)*(1.0)$	0.024
W11	T3T4T5	$(1-0.6)*(1-0.5)*(0.7)*(0.4)*(1.0)$	0.056
W12	T1T2T3T5	$(0.6)*(0.5)*(0.7)*(1-0.4)*(1.0)$	0.126
W13	T1T2T4T5	$(0.6)*(0.5)*(1-0.7)*(0.4)*(1.0)$	0.036
W14	T1T3T4T5	$(0.6)*(1-0.5)*(0.7)*(0.4)*(1.0)$	0.084
W15	T2T3T4T5	$(1-0.6)*(0.5)*(0.7)*(0.4)*(1.0)$	0.056
W16	T1T2T3T4T5	$(0.6)*(0.5)*(0.7)*(0.4)*(1.0)$	0.084

Figure -7: PWS for PDB for Pascal Transactional Temporal Dataset with Probabilistic Confidence  
 The collection of Items for figure 6 PDB contains 6 individual items, let say I is the set of these items. Hence  $I = \{A, B, C, D, E, F\}$ , For this example minsup is 2/5 that is 40%. As total number of transactions in database i.e. the size of database n is 5. So, the threshold for minsup will be given by  $(5 * 40) / 100$ , i.e 2. So, minsup is 2, let minprob is 0. We are taking minprob 0 to show that algorithm will behave exactly as apriori behave when no probabilistic transaction is considered. This is equivalent to treating all transactions having certainty or probability of 1 to occur. All the elements which belongs to collection I will become the candidate pattern, as the individual items themselves are used as patterns we call them 1-itemset. The collection of candidate 1-itemset denoted as  $C_1$  is as follows:  $C_1 = \{ \{A\}, \{B\}, \{C\}, \{D\}, \{E\}, \{F\} \}$  for each element c belongs to  $C_1$  we calculate its support in database PDB Figure 6. For all itemset the PDB database scan output is as follows:

Pattern/1-itemset	Support in PDB
{A}	3
{B}	4
{C}	4
{D}	1
{E}	4
{F}	5

Figure -8:  $C_1$  and its Support Count

In the figure 8 if we compare support of respective patterns we found that pattern {D} has a support 1 which is less than the minimum support.  $sup(\{D\}) < minsup$ . So the set of frequent 1-itemset  $FP_1$  will contain all 1-itemset from figure 8 but not {D}. This set of frequent 1-itemset  $FP_1$  is as follows;

Pattern/1-	Support in PDB
------------	----------------

itemset	
{A}	3
{B}	4
{C}	4
{E}	4
{F}	5

Figure -9: FP<sub>1</sub> set of frequent 1-itemset

Now we use patterns in FP<sub>1</sub> one by one to calculate their existential probability. For this we first scan PDB and extract the TIDs in which pattern is present. For combination of length equal to in range for support from 0 to c.support we start scan of PWS rows and sum up the provabilities of Wi in which exactly the number of transaction present, here the number of transaction which occurred in Wi is determined for every support from 0 to c.support. For example we want to determine existential probability of frequent 1-itemset {A} to determine probabilistic frequent pattern {A} is or not. First, we scan PDB and found that T1, T3, T5 contains {A}. {A}.support is 3. So for transaction combination length of 0, 1, 2, and 3, are possible k th support for {A} in PDB. Let say for example support 1 of pattern {A}, exactly for the count of 1, number of transactions that have {A}, Wi will form universe, means any Wi that contain exactly one time any of the {A}.Ti, i.e., Wi exactly contain either one of T1, or T2, or T2 but not T1T2, T1T3 or T2T3 or T1T2T3 together, all their probabilities will be summed up. For {A}.support is 1, PWS is W1W3W5W10 with probability 0.036, 0.036, 0.024, 0.024 summed up to 0.12, this 0.12 is existential probability of pattern {A} when its support is 1. Like wise we calculate for all fp belongs to FP<sub>1</sub>. The following figure 10 summaries C<sub>1</sub> PFP<sub>1</sub> patterns with their support pmf values. "-" represents not required status.

Support\Pattern	{A}	{B}	{C}	{D}	{E}	{F}
0	0	0	0	0.4	0	0
1	0.12	0.09	0.06	0.6	0.09	0.036
2	0.46	0.36	0.29	-	0.36	0.198
3	0.42	0.41	0.44	-	0.41	0.380
4	-	0.14	0.21	-	0.14	0.246
5	-	-	-	-	-	0.140

Figure -10: C<sub>1</sub> candidate PFP<sub>1</sub> patterns with their support pmf values

If we compare all 1-itemset support pmf values against minprob we will get PFP 1-itemset. For minprob "0" we will have entire Figure 10 as probabilistic frequent PFP<sub>1</sub>. So, now using all patterns in PFP<sub>1</sub> we will continue and

assign this collection to L<sub>1</sub> and call apriori\_gen on all probabilistically frequent 1-itemset patterns in L<sub>1</sub> to generate candidate 2-itemset C<sub>2</sub>. Using PDB database scan we count their support.

Pattern/2-itemset	Support in PDB
{AB}	2
{AC}	3
{AE}	2
{AF}	3
{BC}	3
{BE}	4
{BF}	4
{CE}	3
{CF}	4
{EF}	4

Figure -11: C<sub>2</sub> and its Support Count

All pattern in Figure 11 are frequent. So, frequent 2-itemset will be as following in figure 12.

Pattern/2-itemset	Support in PDB
{AB}	2
{AC}	3
{AE}	2
{AF}	3
{BC}	3
{BE}	4
{BF}	4
{CE}	3
{CF}	4
{EF}	4

Figure -12: FP<sub>2</sub> and its Support Count

The candidate for PFP will be as following in figure 13.

Pattern>SupportV	{A B}	{A C}	{A E}	{A F}	{B C}	{B E}	{B F}	{C E}	{C F}	{E F}
0	0	0	0	0	0	0	0	0	0	0
1	0.32	0.13	0.3	0.12	0.15	0.09	0.09	0.15	0.06	0.09
2	0.76	0.46	0.7	0.46	0.50	0.36	0.36	0.50	0.29	0.36
3	-	0.4	-	0.4	0.3	0.4	0.4	0.3	0.4	0.4

		2		2	5	1	1	5	4	1
4	-	-	-	-	-	0.1 4	0.1 4	-	0.2 1	0.1 4
5	-	-	-	-	-	-	-	-	-	-

Figure -13: C<sub>2</sub> candidate PFP<sub>2</sub> patterns with their support pmf values.

All candidate PFP<sub>2</sub> are probabilistic frequent hence we treat patterns in figure 13 as PFP and finally as L<sub>2</sub>. These 2-itemset probabilistically frequent patterns in L<sub>2</sub> will be used to generate candidate 3-itemset patterns.

Pattern/3-itemset	Support in PDB
{ABC}	2
{ABE}	2
{ABF}	2
{ACE}	2
{ACF}	3
{AEF}	2
{BCE}	3
{BCF}	3
{BEF}	4
{CEF}	3

Figure -14.: C<sub>3</sub> and its Support Count

All pattern in Figure 14 are frequent. So, frequent 3-itemset will be as following in figure 15.

Pattern/3-itemset	Support in PDB
{ABC}	2
{ABE}	2
{ABF}	2
{ACE}	2
{ACF}	3
{AEF}	2
{BCE}	3
{BCF}	3
{BEF}	4
{CEF}	3

Figure -15: FP<sub>3</sub> and its Support Count

The candidate for PFP will be as following in figure 16.

Patt	{A}	{AB}	{A}	{AC}	{AC}	{A}	{BC}	{B}	{B}	{B}	{CE}
------	-----	------	-----	------	------	-----	------	-----	-----	-----	------

ern Support	BC }	E} }	BF }	E} }	F} }	EF }	E} }	CF }	EF }
0	0	0	0	0	0	0	0	0	0
1	0.2 64	0.2 64	0.2 64	0.2 64	0.2 64	0.2 64	0.1 5	0.1 5	0.0 9
2	0.7 36	0.7 36	0.7 36	0.7 36	0.7 36	0.7 36	0.5 0	0.5 0	0.3 6
3	-	-	-	-	-	-	0.3 5	0.3 5	0.4 1
4	-	-	-	-	-	-	-	-	0.1 4
5	-	-	-	-	-	-	-	-	-

Figure -16: C<sub>3</sub> candidate PFP<sub>3</sub> patterns with their support pmf values.

All candidate PFP<sub>3</sub> are probabilistic frequent hence we treat patterns in figure 16 as PFP and finally as L<sub>3</sub>. These 3-itemset probabilistically frequent patterns in L<sub>3</sub> will be used to generate candidate 4-itemset patterns, which are as follows;

Pattern/4-itemset	Support in PDB
{ABCE}	2
{ABCF}	2
{ABEF}	2
{ACEF}	2
{BCEF}	3

Figure -17: C<sub>4</sub> and its Support Count

All pattern in Figure 17 are frequent. So, frequent 3-itemset will be as following in figure 18.

Pattern/4-itemset	Support in PDB
{ABCE}	2
{ABCF}	2
{ABEF}	2
{ACEF}	2
{BCEF}	3

Figure -18: FP<sub>4</sub> and its Support Count

The candidate for PFP will be as following in figure 19.

Pattern Support	{ABCE}	{ABCF}	{ABEF}	{ACEF}	{BCEF}
0	0	0	0	0	0
1	0.264	0.264	0.264	0.264	0.15
2	0.736	0.736	0.736	0.736	0.50
3	-	-	-	-	0.35
4	-	-	-	-	-
5	-	-	-	-	-

Figure -19: C<sub>4</sub> candidate PFP<sub>4</sub> patterns with their support pmf values.

All candidate PFP<sub>4</sub> are probabilistic frequent hence we treat patterns in figure 19 as PFP and finally as L<sub>4</sub>. These 4-itemset probabilistically frequent patterns in L<sub>4</sub> will be used to generate candidate 5-itemset patterns, which are as follows;

Pattern/4-itemset	Support in PDB
{ABCE}	2

Figure -20: C<sub>5</sub> and its Support Count

All pattern in Figure 20 are frequent. So, frequent 3-itemset will be as following in figure 21.

Pattern/5-itemset	Support in PDB
{ABCEF}	2

Figure -21: P<sub>5</sub> and its Support Count

The candidate for PFP will be as following in figure 22.

Support\Pattern	{ABCEF}
0	0
1	0.264
2	0.736
3	-
4	-
5	-

Figure -22: C<sub>5</sub> candidate PFP<sub>5</sub> patterns with their support pmf values.

All candidate PFP<sub>5</sub> are probabilistic frequent hence we treat patterns in figure 22 as PFP and finally as L<sub>5</sub>. These 5-itemset probabilistically frequent patterns in L<sub>5</sub> will be used to generate candidate 6-itemset patterns. But no

more new candidate 6-itemset are possible so algorithm execution stops here.

### 5. CONCLUSION

Real world application requires mining of patterns occurrences of which are random or uncertain in nature. This uncertain is introduced in the system because of many parameters which may be endogenous or exogenous. This uncertainty is introduced many time because of uncertainty in competency of operator involved in transactional process. Uncertainty may be introduced due to limitation of measurement machines, instruments, and/or procedure. So, to encompass this truth of process we studied and suggested a mining procedure that can be used to answer queries which or otherwise only possible to answer on certain data using data mining techniques. To best of our knowledge the steps we carried out are not discuss to this much extent in any paper. Algorithm finally converged. 32 probabilistic frequent patterns were generated when we took the probability of transactions equal to one, i.e. minimum threshold is considered as 0. Many variations in implementation of the algorithm are possible. Also how to select suitable minprob threshold is, depending on this algorithm can be modified. In future we will implement the algorithm with possible alternate implementation as well as mechanism to support selection of minimum support threshold, and selection of minimum probability threshold.

### REFERENCES

[1] R. Agrawal, C. Faloutsos, and A. Swami. Efficient similarity search in sequence databases. In Proc. of the Fourth International Conference on Foundations of Data Organization and Algorithms, Chicago, October 1993.

[2] R. Agrawal, S. Ghosh, T. Imielinski, B. Iyer, and A. Swami. An interval classifier for database mining applications. In Proc. of the VLDB Conference, pages 560{573, Vancouver , British Columbia, Canada, 1992.

[3] R. Agrawal, T. Imielinski, and A. Swami. Database mining: A performance perspective. IEEE Transactions on Knowledge and Data Engineering, 5(6):914{925, December 1993. Special Issue on Learning and Discovery in Knowledge- Based Databases.

[4] R. Agrawal, T. Imielinski, and A. Swami. Mining association rules between sets of items in large databases. In Proc. of the ACM SIGMOD Conference on Management of Data, Washington, D.C., May 1993.

[5] R. Agrawal and R. Srikant. Fast algorithms for mining association rules in large databases. Research Report RJ 9839, IBM Almaden Research Center, San Jose, California, June 1994.

[6] D. S. Associates. The new direct marketing. Business One Irwin, Illinois, 1990.

[7] R. Brachman et al. Integrated support for data archeology. In AAAI-93 Workshop on Knowledge Discovery in Databases, July 1993.

- [8] L. Breiman, J. H. Friedman, R. A. Olshen, and C. J. Stone. Classification and Regression Trees. Wadsworth, Belmont, [9] P. Cheeseman et al. Autoclass: A bayesian classification system. In 5th Int'l Conf. on Machine Learning. Morgan Kaufman, June 1988.
- [10] D. H. Fisher. Knowledge acquisition via incremental conceptual clustering. Machine Learning, 2(2), 1987.
- [11] J. Han, Y. Cai, and N. Cercone. Knowledge discovery in databases: An attribute oriented approach. In Proc. of the VLDB Conference, pages 547{559, Vancouver, British Columbia, Canada, 1992.
- [12] M. Holsheimer and A. Siebes. Data mining: The search for knowledge in databases. Technical Report CS-R9406, CWI, Netherlands, 1994.
- [13] M. Houtsma and A. Swami. Set-oriented mining of association rules. Research Report RJ 9567, IBM Almaden Research Center, San Jose, California, October 1993.
- [14] R. Krishnamurthy and T. Imielinski. Practitioner problems in need of database research: Research directions in knowledge discovery. SIGMOD RECORD, 20(3):76{78, September 1991.
- [15] P. Langley, H. Simon, G. Bradshaw, and J. Zytkow. Scientific Discovery: Computational Explorations of the Creative Process. MIT Press, 1987.
- [16] H. Mannila and K.-J. Raiha. Dependency inference. In Proc. of the VLDB Conference, pages 155{158, Brighton, England, 1987.
- [17] H. Mannila, H. Toivonen, and A. I. Verkamo. Efficient algorithms for discovering association rules. In KDD-94: AAAI Workshop on Knowledge Discovery in Databases, July 1994.
- [18] S. Muggleton and C. Feng. Efficient induction of logic programs. In S. Muggleton, editor, Inductive Logic Programming. Academic Press, 1992.
- [19] J. Pearl. Probabilistic reasoning in intelligent systems: Networks of plausible inference, 1992.
- [20] G. Piatetsky-Shapiro. Discovery, analysis, and presentation of strong rules. In G. Piatetsky-Shapiro, editor, Knowledge Discovery in Databases. AAAI/MIT Press, 1991.
- [21] G. Piatetsky-Shapiro, editor. Knowledge Discovery in Databases. AAAI/MIT Press, 1991.
- [22] J. R. Quinlan. C4.5: Programs for Machine Learning. Morgan Kaufman, 1993.
- [23] Rakesh Agrawal, Ramakrishnan Srikant: "Fast Algorithms for Mining Association Rules" Proceedings of the 20th VLDB Conference Santiago, Chile, 1994
- [24] Liwen Sun, Reynold Cheng, David W. Cheung, Jiefeng Cheng, "Mining Uncertain Data with Probabilistic Guarantees", KDD'10, July 25–28, 2010, Washington, DC, USA. Copyright 2010 ACM 978-1-4503-0055-1/10/07
- [25] A. Deshpande et al. Model-driven data acquisition in sensor networks. In VLDB, 2004.
- [26] C. Aggarwal, Y. Li, J. Wang, and J. Wang. Frequent pattern mining with uncertain data. In KDD, 2009.
- [27] C. Aggarwal and P. Yu. A survey of uncertain data algorithms and applications. IEEE Transactions on Knowledge and Data Engineering, 21(5), 2009.
- [28] R. Agrawal and R. Srikant. Fast algorithms for mining association rules in large databases. Technical report, RJ 9839, IBM, 1994.
- [29] R. Bayardo, Jr. Efficiently mining long patterns from databases. In SIGMOD, 1998.
- [30] D. Burdick, M. Calimlim, J. Flannick, J. Gehrke, and T. Yiu. MAFIA: A maximal frequent itemset algorithm. IEEE Transactions on Knowledge and Data Engineering, 17, 2005.
- [31] H. Cheng, P. Yu, and J. Han. Approximate frequent itemset mining in the presence of random noise. Soft Computing for Knowledge Discovery and Data Mining, 2008.
- [32] R. Cheng, D. Kalashnikov, and S. Prabhakar. Evaluating probabilistic queries over imprecise data. In SIGMOD, 2003.
- [33] C. K. Chui, B. Kao, and E. Hung. Mining frequent itemsets from uncertain data. In PAKDD, 2007.
- [34] G. Cormode and M. Garofalakis. Sketching probabilistic data streams. In SIGMOD, 2007.
- [34] N. Dalvi and D. Suciu. Efficient query evaluation on probabilistic databases. In VLDB, 2004.
- [35] M. Garofalakis and A. Kumar. Wavelet synopses for general error metrics. ACM Transactions on Database Systems, 30(4), 2005.
- [36] K. Gouda and M. J. Zaki. GenMax: An efficient algorithm for mining maximal frequent itemsets. Data Mining and Knowledge Discovery, 11(3), 2005.
- [37] R. Hogg, A. Craig, and J. McKean. Introduction to Mathematical Statistics (6th ed.). Prentice Hall, 2004.
- [38] J. Huang et al. MayBMS: A Probabilistic Database Management System. In SIGMOD, 2009.
- [39] N. Khossainova, M. Balazinska, and D. Suciu. Towards correcting input data errors probabilistically using integrity constraints. In MobiDE, 2006.
- [40] D. Knuth. The art of computer programming, vol. 3. Addison Wesley, 1998.
- [41] H. Kriegel and M. Pfeifle. Density-based clustering of uncertain data. In KDD, 2005.
- [42] C. Kuok, A. Fu, and M. Wong. Mining fuzzy association rules in databases. SIGMOD Record, 1998.
- [43] A. Lu, Y. Ke, J. Cheng, and W. Ng. Mining vague association rules. In DASFAA, 2007.

- [44] M. Mutsuzaki et al. Trio-one: Layering uncertainty and lineage on a conventional dbms. In CIDR, 2007.
- [45] M. Yiu et al. Efficient evaluation of probabilistic advanced spatial queries on existentially uncertain data. IEEE Transactions on Knowledge and Data Engineering, 21(9), 2009.
- [46] R. Motwani and P. Raghavan. Randomized algorithms. Cambridge University Press, New York, NY, USA, 1995.
- [47] A. Oppenheim, R. Schafer, and J. Buck. Discrete-time signal processing (2nd ed.). Prentice Hall, 1999.
- [48] P. Sistla et al. Querying the uncertain position of moving objects. In Temporal Databases: Research and Practice. Springer Verlag, 1998.
- [49] J. Ren, S. Lee, X. Chen, B. Kao, R. Cheng, and D. Cheung. Naïve Bayes Classification of Uncertain Data. In ICDM, 2009.
- [50] T. Bernecker et al. Probabilistic frequent itemset mining in uncertain databases. In KDD, 2009.
- [51] T. Jayram et al. Avatar information extraction system. IEEE Data Engineering Bulletin, 29(1), 2006.
- [52] P. Tan, M. Steinbach, and V. Kumar. Introduction to Data Mining. Pearson Education, 2006.
- [53] C. Yang and W. Najm. Examining driver behavior using data gathered from red light photo enforcement cameras. Journal of Safety Research, 38(3), 2007.
- [54] Q. Zhang, F. Li, and K. Yi. Finding frequent items in probabilistic data. In SIGMOD, 2008.

## BIOGRAPHIES

Niket Bhargava, born in state is MP in the India, on July 6, 1978. He graduated from the Oriental Institute of Science And Technology, Bhopal, and after qualifying in GATE, completed his Master in Technology from the RGTU- the technical university of MP, India. His employment experience included the 10 years as Teacher in Top Most Ranking Institutions of state of MP, and Industry experience of BI product development. Presently, he is pursuing his PhD in CSE with focus on business applications of data mining, data science, big data techniques for Business Intelligence.

Dr. MANOJ SHUKLA, is working as professor in BCE, Mandiddeep. He is having more than 15 years of experience in teaching and hold positions like principal, and others in various institutes in Madhya Pradesh, India.